



Large Eddy Simulation of Airfoil Self-Noise

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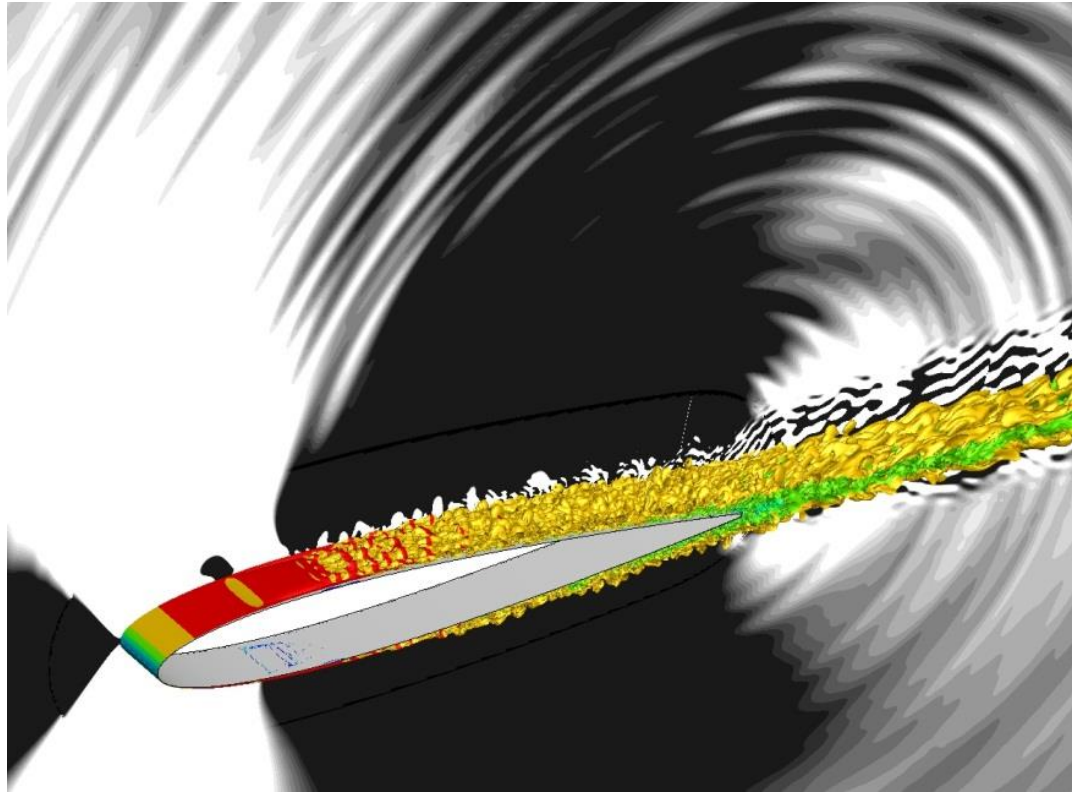
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Department of Aeronautics and Astronautics and

Department of Mechanical Engineering

AMS Seminar Series, 02/09/2016

Introduction



- Noise generated by a turbulent boundary layer that encounters the trailing edge of an airfoil

Motivation



The need for HPC



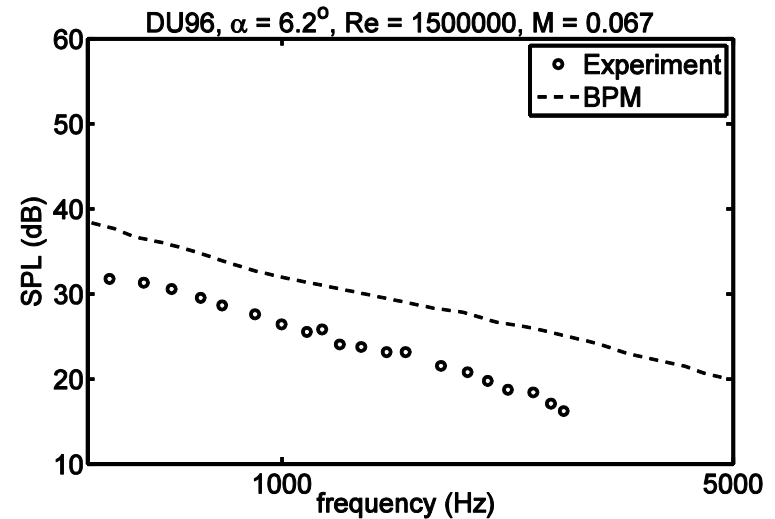
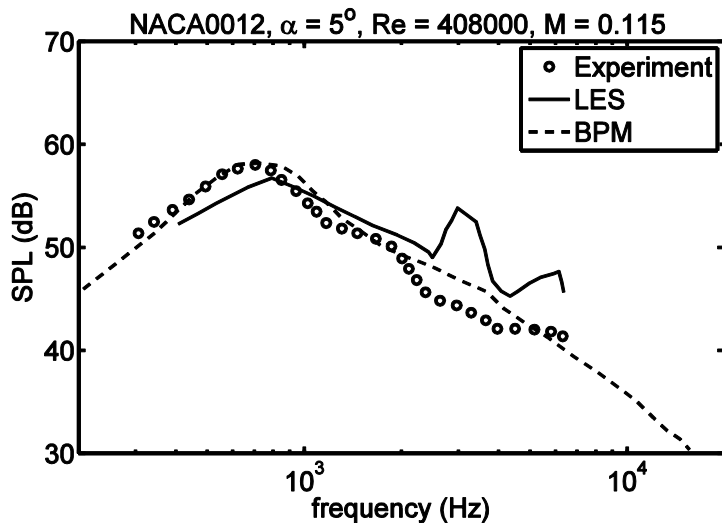
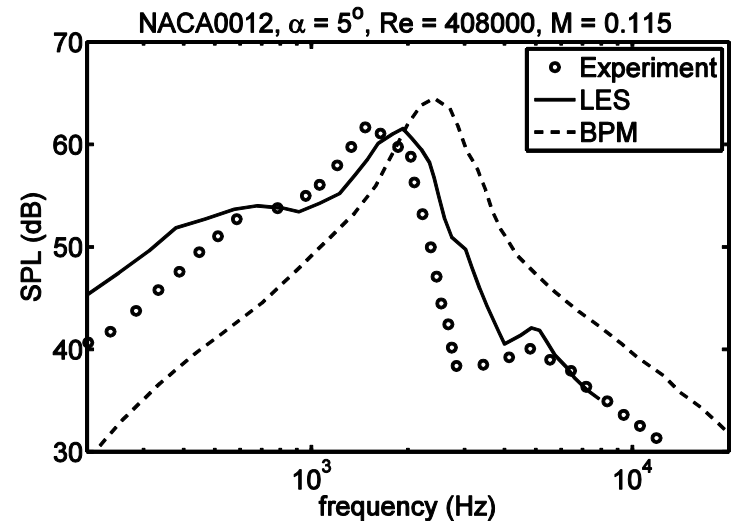
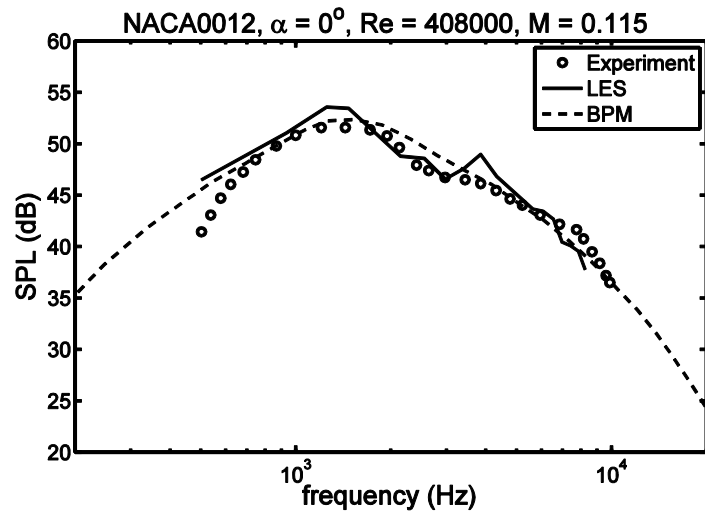
- Trailing edge noise dominates modern wind turbine noise
- Are semi-empirical wind turbine noise prediction methods robust enough?
- RANS not reliable for predicting aerodynamic stall
- Aerodynamics and acoustics from first principles – a pacing item and a challenge

The need for HPC



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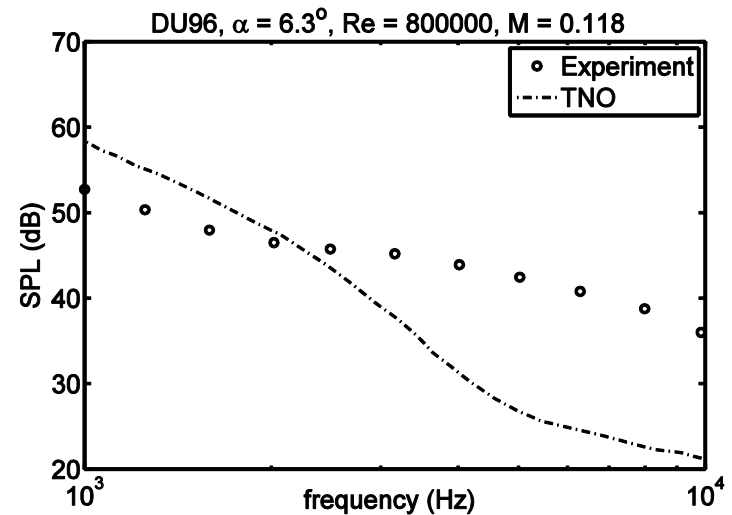
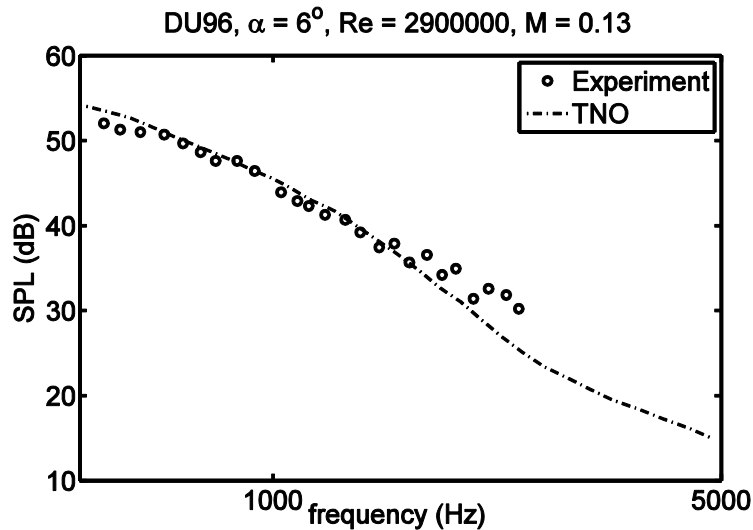
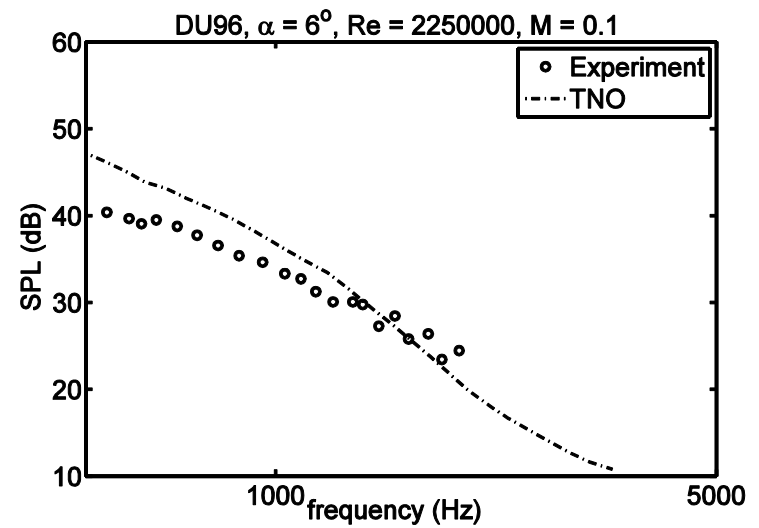
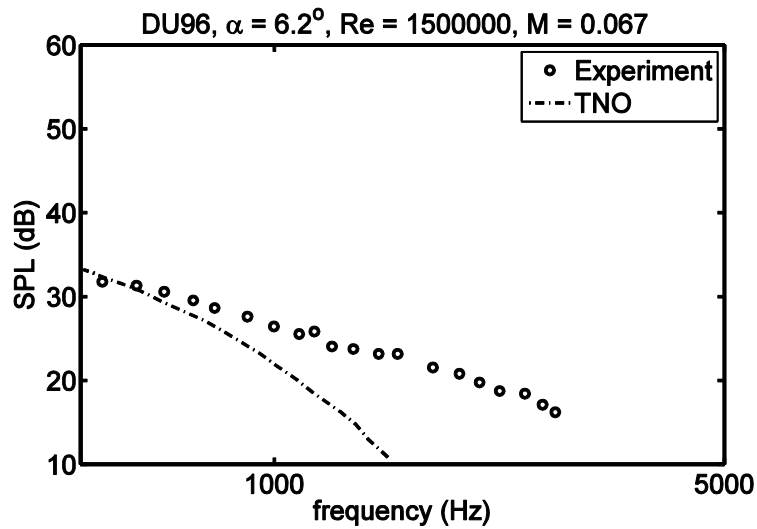
Engineering Models: BPM



LES: Wolf *et al.*, 2012

Exp: Brooks *et al.*, 1989, Devenport *et al.*, 2010

Engineering Models: TNO



Exp: Devenport *et al.*, 2010, Herr and Pott-Pollenske, 2011

EUDP Project 'Low Noise Airfoil' – Final Report

Author: BERTAGNOLIO Franck (Editor)
Title: EUDP Project 'Low Noise Airfoil' - Final Report
Department: DTU Wind Energy

Report number:
DTU Wind Energy-E- 0004
Publication date:
June 2012

Finally, a new airfoil design was proposed based on a design concept including noise reduction. The new airfoil proved to perform better aerodynamically but noise reduction were not as important as expected, mainly due to the inaccuracy of the simplified flow model used in the design algorithm.

The need for HPC



- Trailing edge noise dominates modern wind turbine noise
- Are semi-empirical wind turbine noise prediction methods robust enough?
- RANS not reliable for predicting aerodynamic stall
- **Aerodynamics and acoustics from first principles – a pacing item and a challenge**

Numerical Simulation of Airfoil Self-Noise: Where are we?

- Significant progress in last 15 years
- Canonical configurations at low to moderate Reynolds numbers *routine*
- Full-scale Reynolds numbers challenging – Lack of synergy between experiments and simulations
- Non-canonical configurations – Stall Noise, Airfoil Tones etc poorly understood

Numerical Simulation of Airfoil Self-Noise: Where are we?

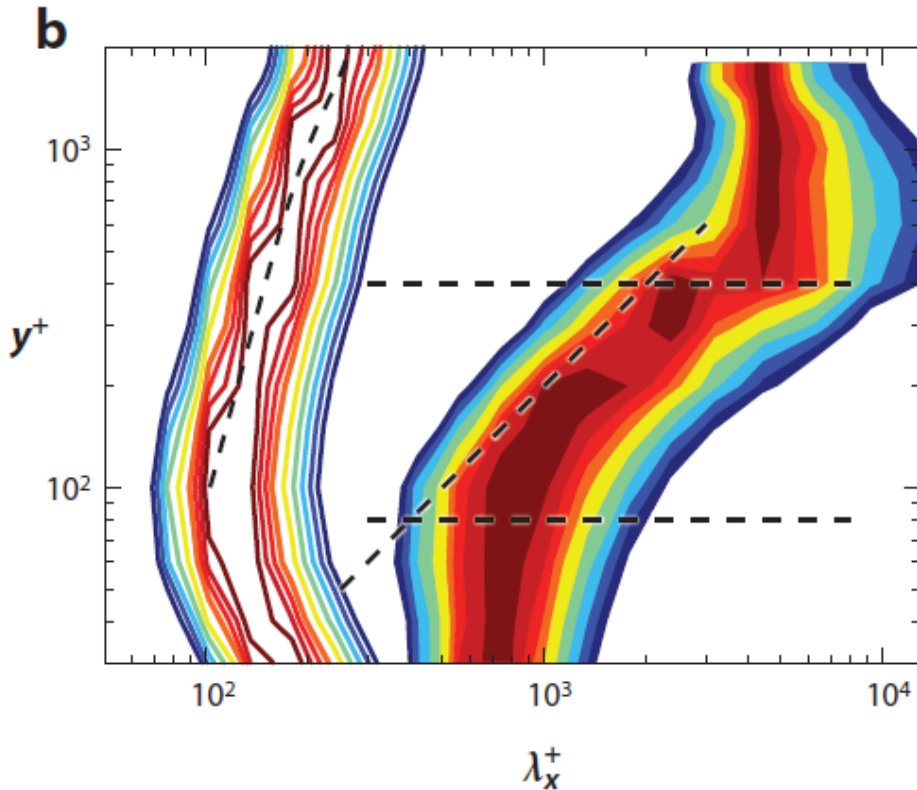
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Wind turbine noise predictions: The challenge of high Reynolds number

Contributors	Year	Configuration	Number of grid points
Wang <i>et al.</i> (LES)	2009	CD airfoil $Re_c = 1.5 \times 10^5$	~ 5 Million
Moon <i>et al.</i> (LES)	2010	Flat Plate $Re_c = 1.3 \times 10^5$	~ 3 Million
Winkler <i>et al.</i> (LES)	2012	NACA 6512-63 $Re_c = 1.9 \times 10^5$	~ 3 Million
Wolf <i>et al.</i> (LES)	2012	NACA 0012 $Re_c = 4.08 \times 10^5$	~ 54 Million
Jones and Sandberg (DNS)	2012	NACA 0012 with serrated TE $Re_c = 5 \times 10^4$	~ 170 Million
GE-Stanford Project	2012	DU96 $Re_c = 1.5 \times 10^6$	~127 – 180 Million

- WRLES of airfoil trailing edge noise restricted to low Reynolds numbers
- NREL 5MW offshore wind turbine – $R = 63\text{m}$, $V = 9\text{m/s}$, $\omega = 1.08\text{rad/s}$, $r = 7.55$, $Re(r = 3/4R) = 12 \times 10^6$
 R – rotor radius
 V -wind speed
 ω – rotation rate
 r - tip speed ratio

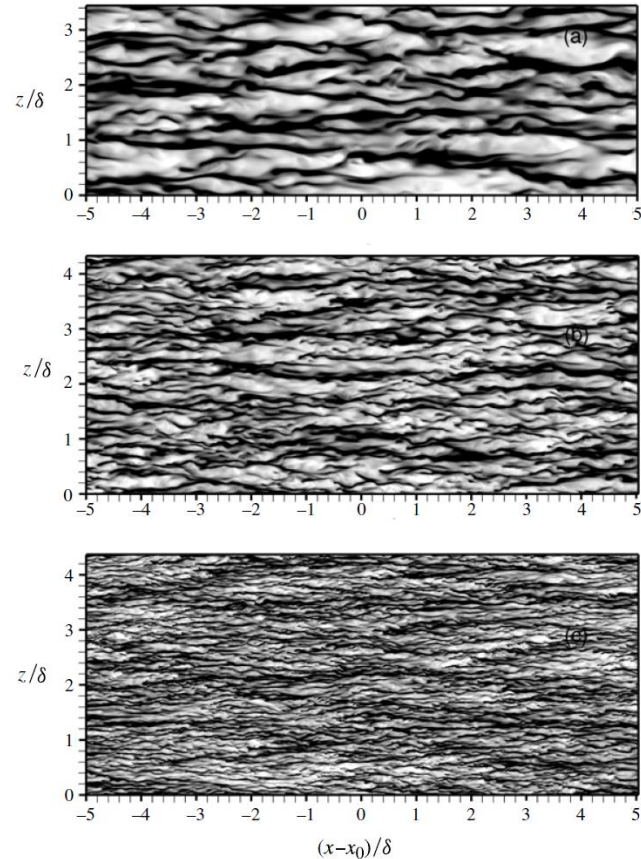
LES of a wall bounded turbulent flow – The challenge of high Reynolds number



Filled contours – co-spectra of tangential Reynolds stress (production), Line contours – Spectra of vorticity magnitude (surrogate for dissipation). Results from DNS of turbulent channel flow at a friction Reynolds number of 2000

- Scale disparity between production and dissipation exists only away from the wall
- Wall Resolved LES grid needs to be very fine close to a wall
- Consequence - Number of grid points (N_g) $\propto Re_x^{13/7}$
- Wall Resolved LES is prohibitively expensive at large Reynolds numbers

Addressing the challenge of high Reynolds number



Instantaneous streamwise velocity from DNS of a turbulent boundary layer at $y^+ = 15$. Friction Reynolds numbers (top to bottom) - 251, 497, 1116

- The scale disparity between *outer* and *inner* scales responsible for $N_g \propto Re_x^{13/7}$
- Remedy - *inner* scales not resolved
- Effect on *outer* scales modeled using a stress boundary condition
- *Outer* eddies scale with the local boundary layer thickness – weak dependence on Re_x
- Consequence - Number of grid points (N_g) $\propto Re_x$

- Introduction
- Why Wall Modeled LES (WMLES)?
- WMLES Methodology
- WMLES of canonical flows
- WMLES of non-canonical flows
- WMLES of trailing edge noise at high Re
- WMLES of noise generated by an airfoil in near stall
- WMLES of flow past a wind turbine airfoil in the post stall regime
- Conclusions
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WMLES methodology

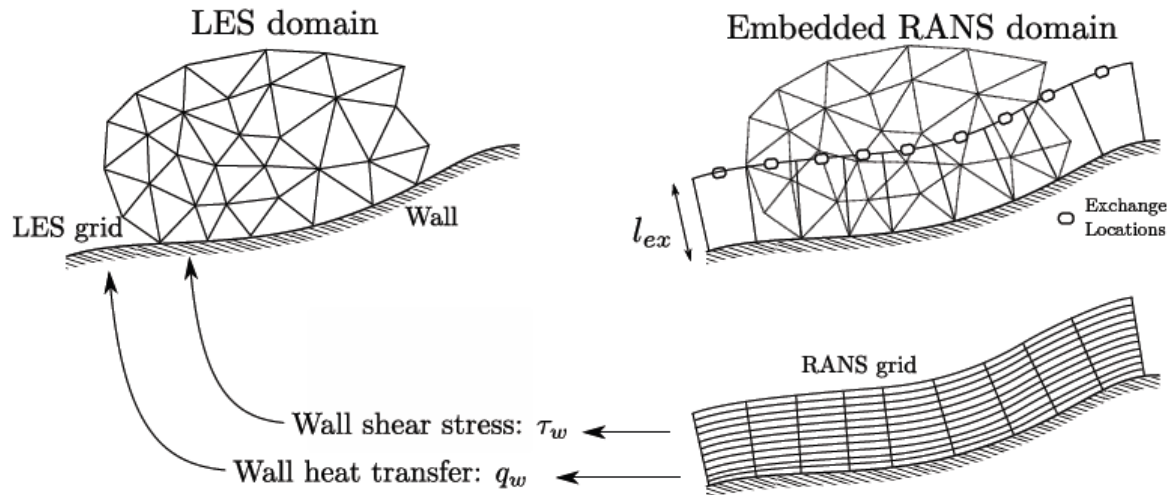


FIGURE 1. Sketch of the wall-modeling procedure.

- Compressible or *Weakly* Compressible Navier-Stokes equations with constant coefficient Vreman sub-grid scale model on the LES grid
- Time-independent ODEs in wall normal direction based on the equilibrium assumption and an algebraic eddy viscosity model with wall damping for turbulence on the RANS grid

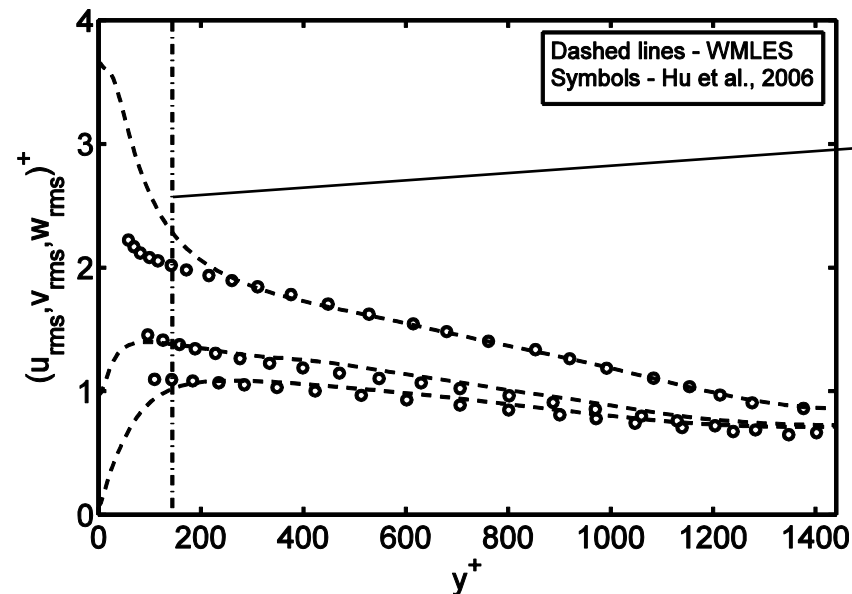
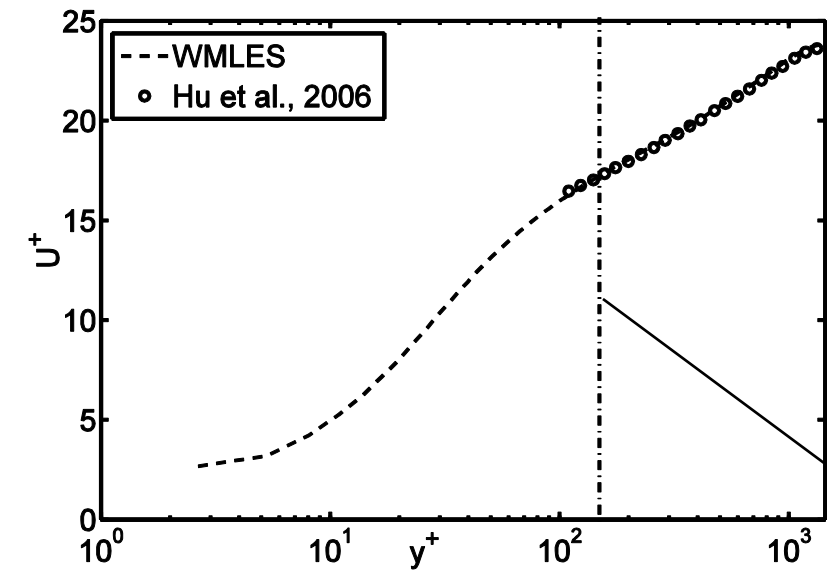
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WMLES of turbulent channel flow

- Flow driven by a body force
- Periodic BCs in streamwise and spanwise directions
- Stress BC from wall model at the walls
- Results validated by comparison with DNS data
- Friction Reynolds number – 1440

WMLES of turbulent channel flow, $Re_\tau \sim 1440$, DNS \sim 500M points, WMLES \sim 1M points

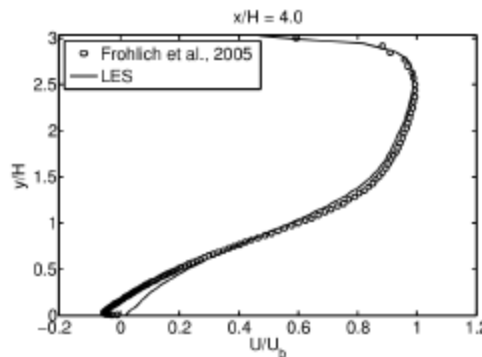
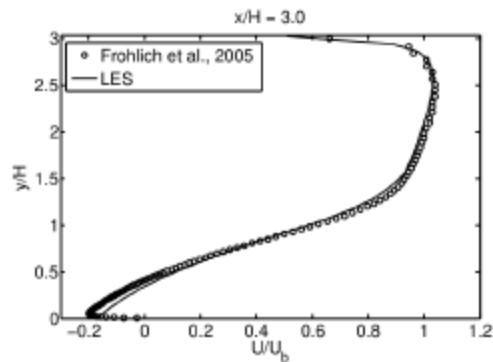
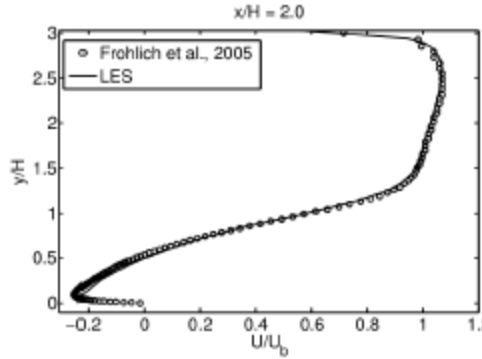
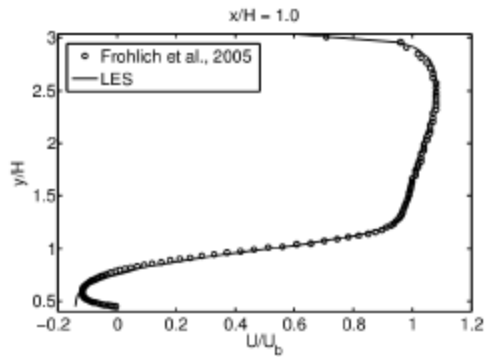
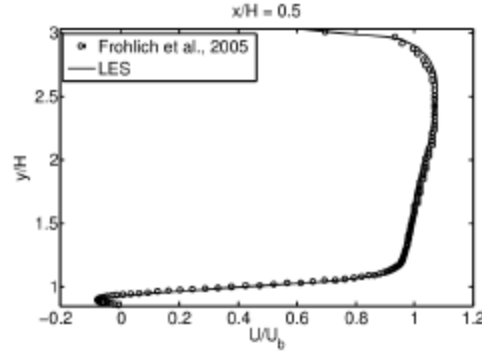
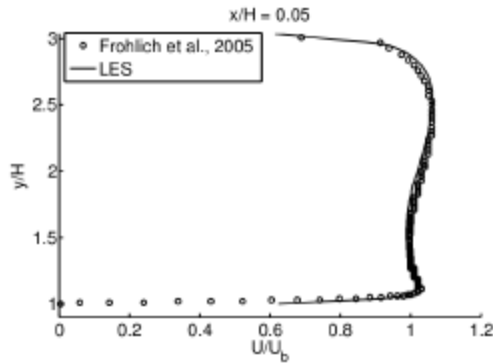


WM matching location

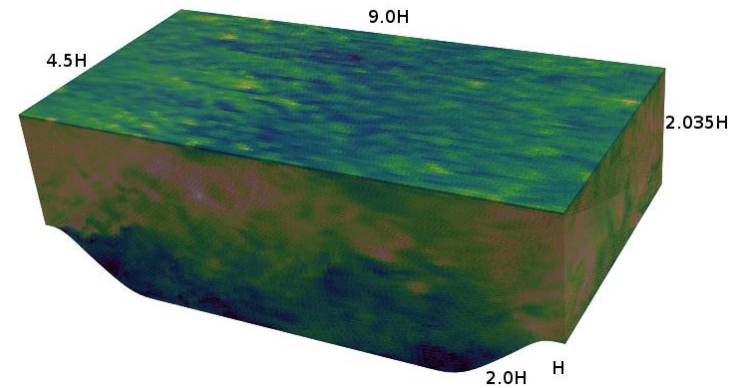
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WMLES of separated flows



WMLES $\sim 0.5\text{M}$ points
WRLES $\sim 12\text{M}$ points
DNS $\sim 200\text{M}$ points



Aerodynamic Aspects of Wind Energy Conversion

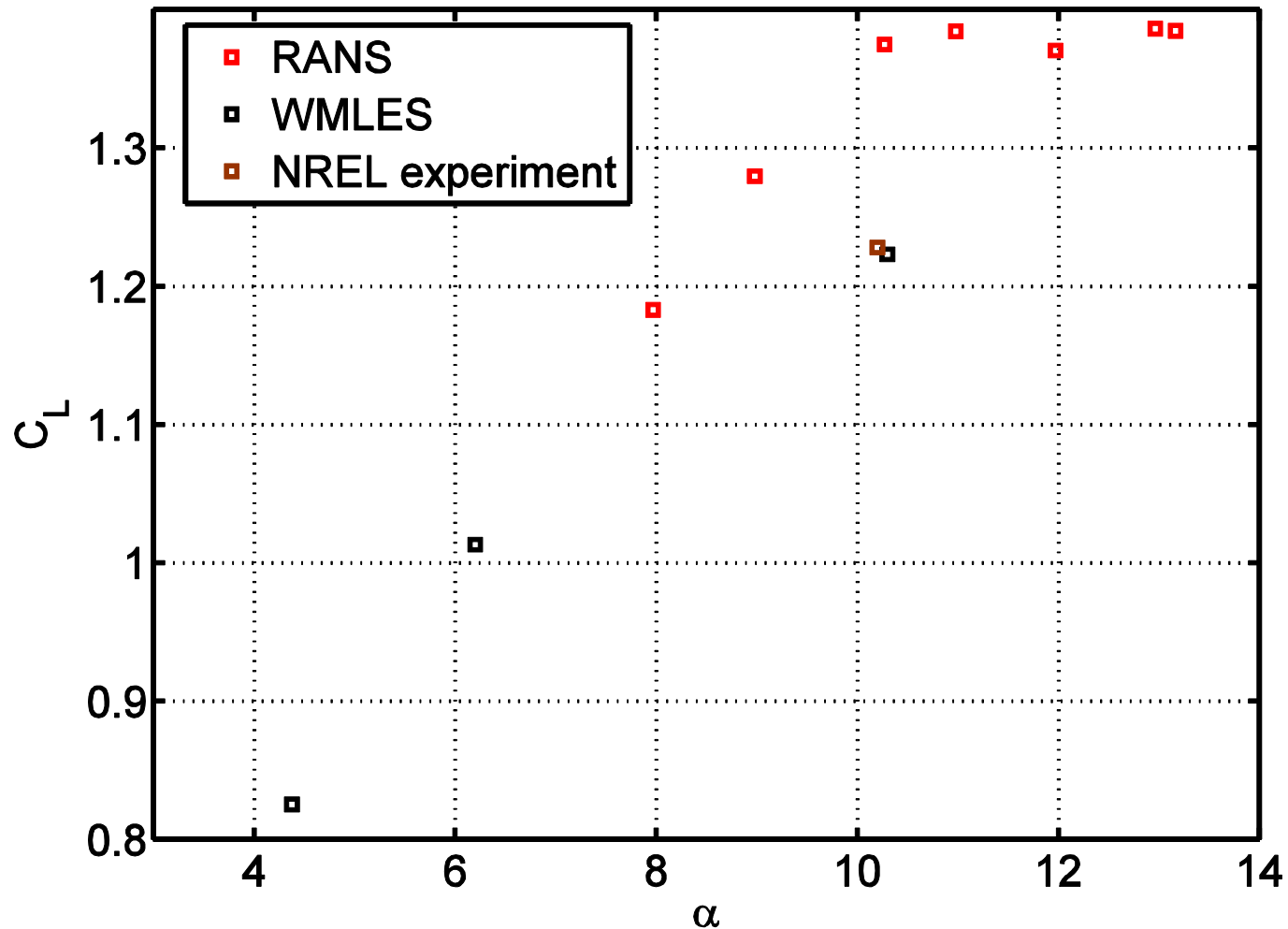
Jens Nørkær Sørensen

Department of Mechanical Engineering, Technical University of Denmark, DK-2800 Kongens Lyngby, Denmark; email: jns@mek.dtu.dk

Annu. Rev. Fluid Mech. 2011. 43:427–48

“The NREL experiments have achieved significant new insight into wind turbine aerodynamics and revealed **serious shortcomings in present-day wind turbine aerodynamics prediction tools**. The Navier-Stokes computations generally exhibited **good agreement** with the measurements **up to wind speeds of approximately 10ms^{-1}** . At this wind speed, flow separation sets in, and for **higher wind speeds**, the boundary layer characteristics are **dominated by stall** and the computations under-predict the power yield.”

Predicting wind turbine stall using WMLES



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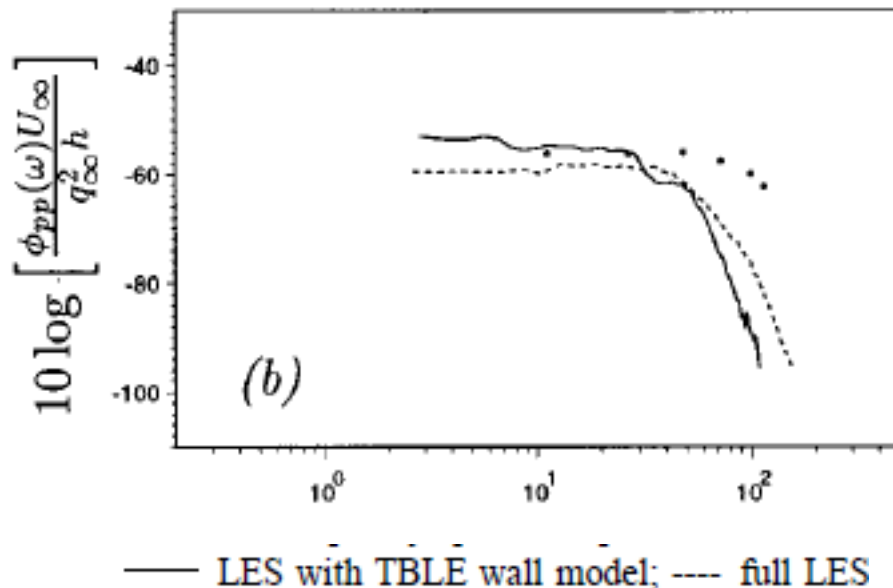
Over-prediction of fluctuating wall pressure and noise in WMLES

Dynamic wall modeling for large-eddy simulation of complex turbulent flows

Meng Wang^{a)} and Parviz Moin

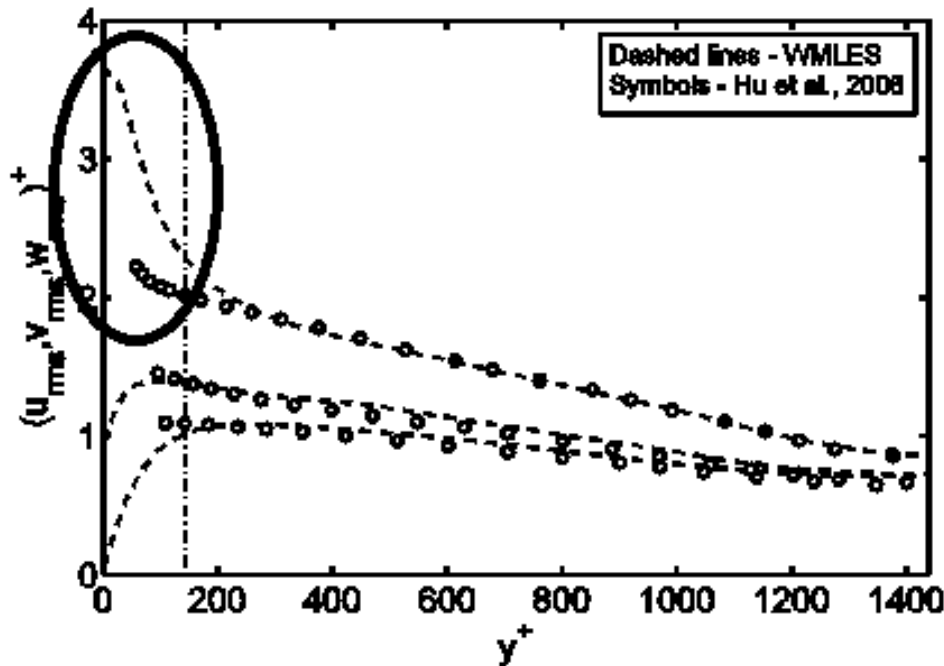
*Center for Turbulence Research, NASA Ames Research Center/Stanford University, MS 19-44,
Moffett Field, California 94035*

(Received 30 January 2001; accepted 18 March 2002; published 17 May 2002)



“Of particular interest in aeronautical and naval applications is the predictive capability of the method for **surface pressure fluctuations** and **noise radiation**. However, relative to the full LES spectra, the **spectral levels** are somewhat **overpredicted**, particularly in the attached flow region [Figs. 14(a)-14(c)]”

Over-prediction of turbulence intensity close to the wall

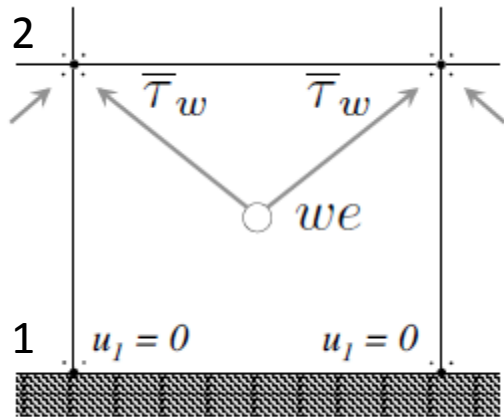


Results from WMLES of turbulent flow in a channel at a friction Reynolds number of 1440.

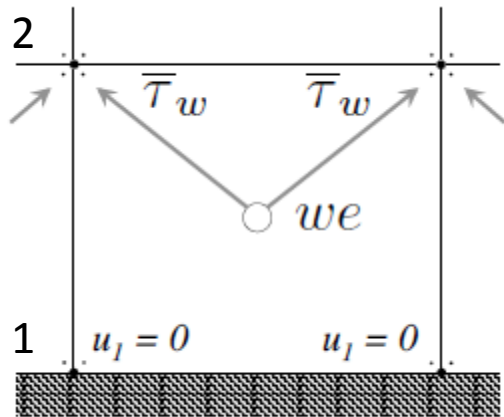
- What does the stress BC do to the structure of *attached* eddies close to the wall?
- Stress BC from wall model does not constrain tangential components of fluctuating velocity to vanish at the wall
- Attached eddies slosh at the wall

How can it be fixed?

$$\tau_w = (\mu + \mu_{sgs}) (u_2 - u_1) / \Delta y$$

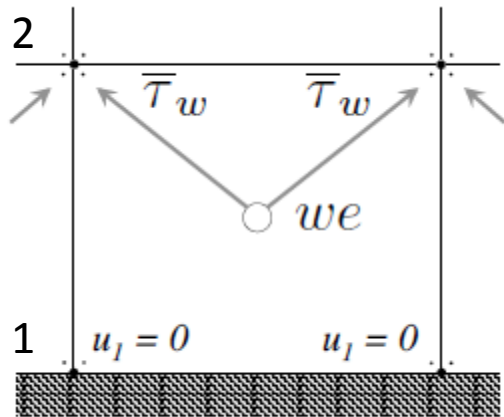


How can it be fixed?



$$\tau_w = (\mu + \mu_{sgs}) (u_2 - 0) / \Delta y$$

How can it be fixed?

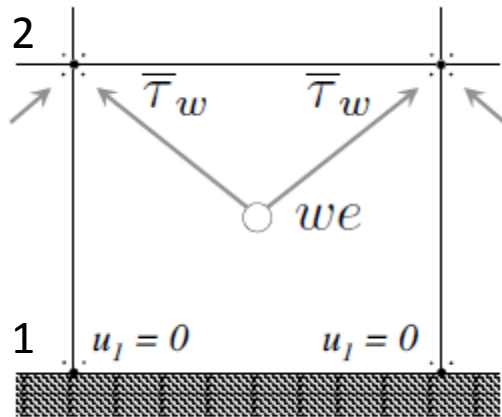


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μ_t

Augment μ_t to enforce the shear stress from the wall model

How can it be fixed?



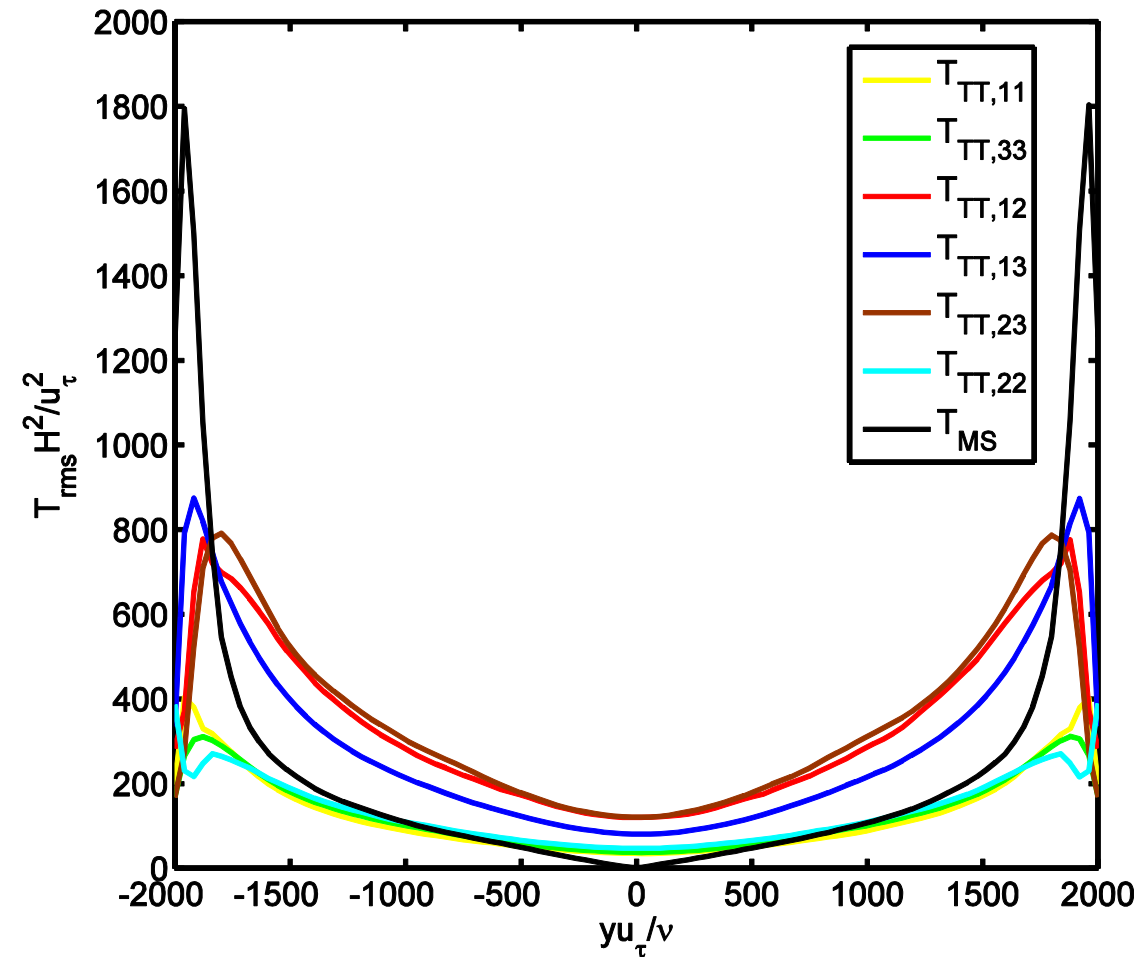
$$\tau_w = (\mu + \mu_{sgs}) (u_2 - 0) / \Delta y$$

μ_t

Augment μ_t to enforce the shear stress from the wall model

- *No slip* enforced at the wall
- Viscosity artificially augmented at the wall to enforce the shear stress from the wall model
- Does it improve prediction of fluctuating wall pressure? Yes
- Does it fix the issue altogether? Not quite

Budget of Poisson equation for fluctuating pressure



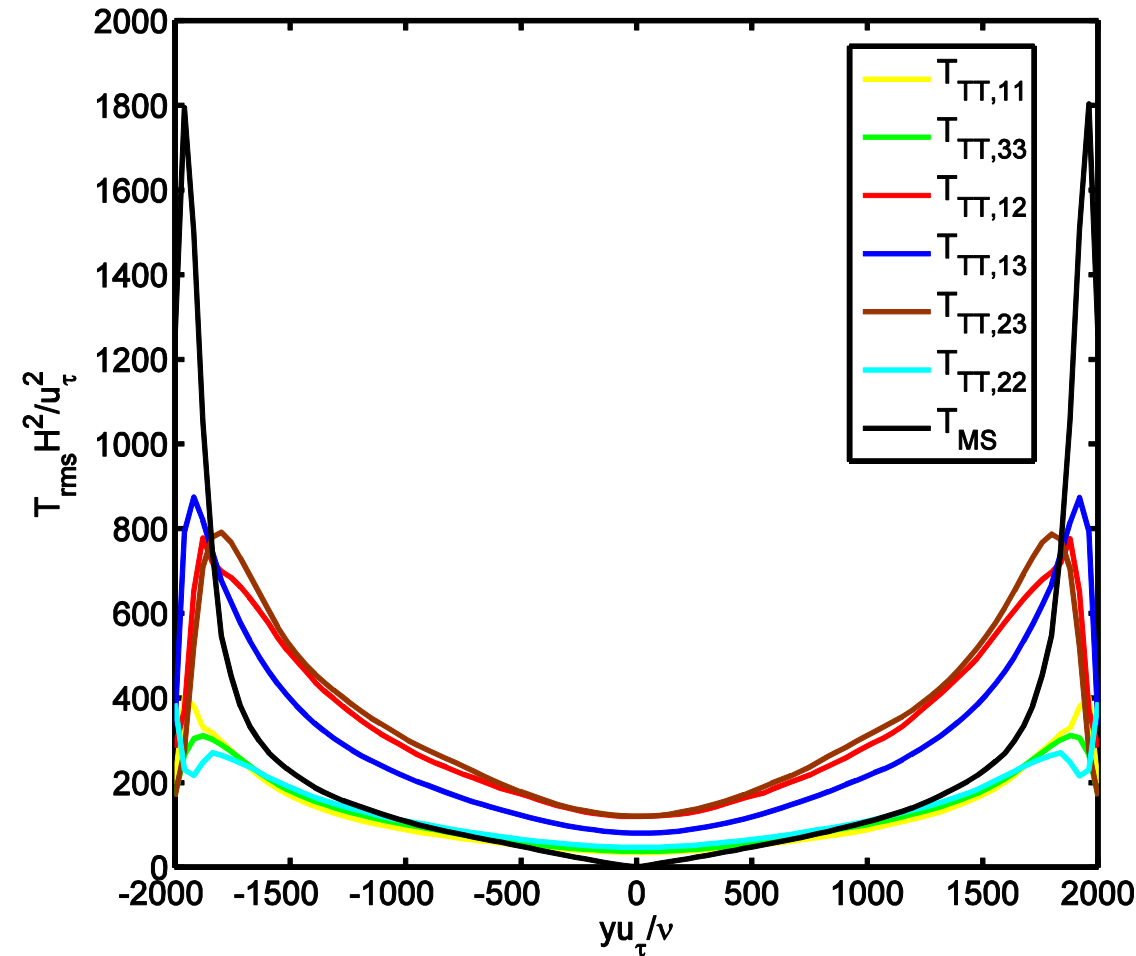
$$\frac{\partial^2 p}{\partial x_i \partial x_i} = -\{T^{\text{MS}} + T^{\text{TT}}\}$$

$$T^{\text{MS}} = 2 \frac{\partial U}{\partial y} \frac{\partial v}{\partial x}$$

- Turbulence-mean shear interaction (Rapid) term over-predicted close to the wall

From WMLES of turbulent flow in a channel at a friction Reynolds number of 2000.

Budget of Poisson equation for fluctuating pressure



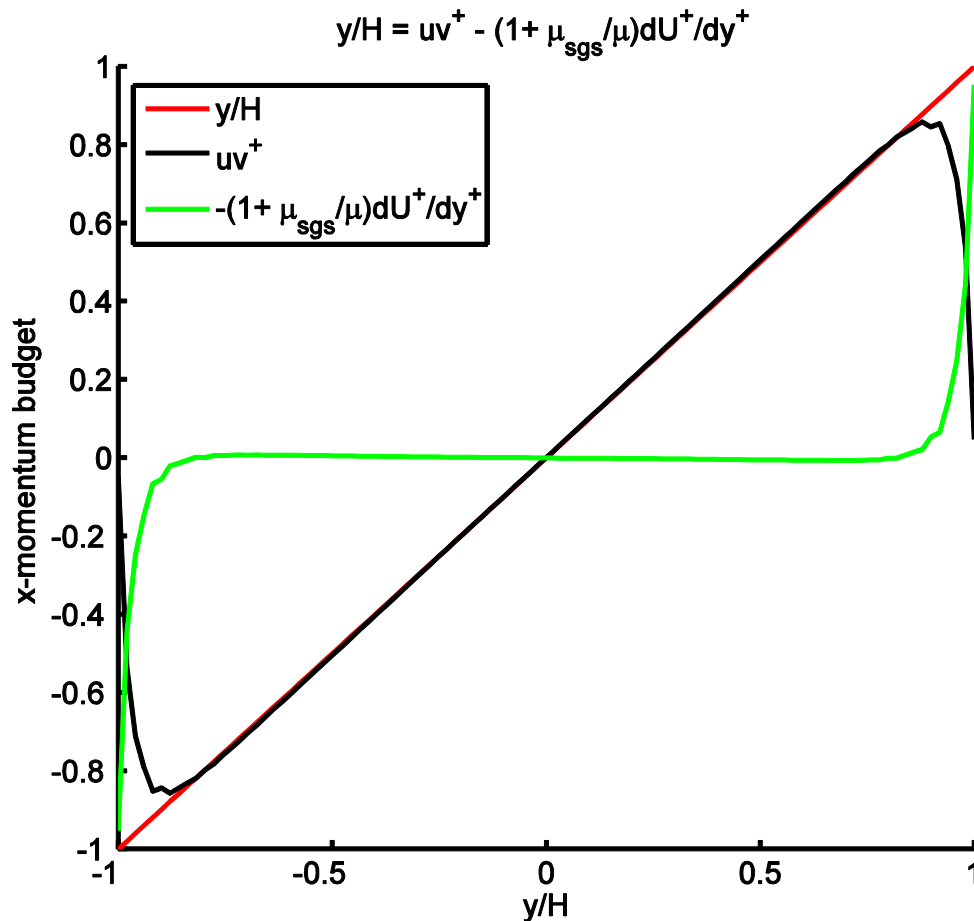
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- Turbulence-mean shear interaction (Rapid) term over-predicted close to the wall
- Why?

Mean x-momentum balance



From WMLES of turbulent flow in a channel at a friction Reynolds number of 2000.

- Reynolds shear stress under-predicted close to the wall
- Subgrid scale model does not contribute *enough* (Not a RANS model)
- Flux from the wall sustained through a higher value of mean velocity gradient

Can the error be fixed? How does it respond to grid refinement?

- To solve the issue, numerical and subgrid scale model errors at the first few off-wall points need to be addressed – *Even a perfect wall stress model won't suffice*
- A posteriori correction possible, but not practical
- *The over-prediction reduces on finer grids* as the Reynolds shear stress starts contributes more to the momentum balance in the vicinity of the wall

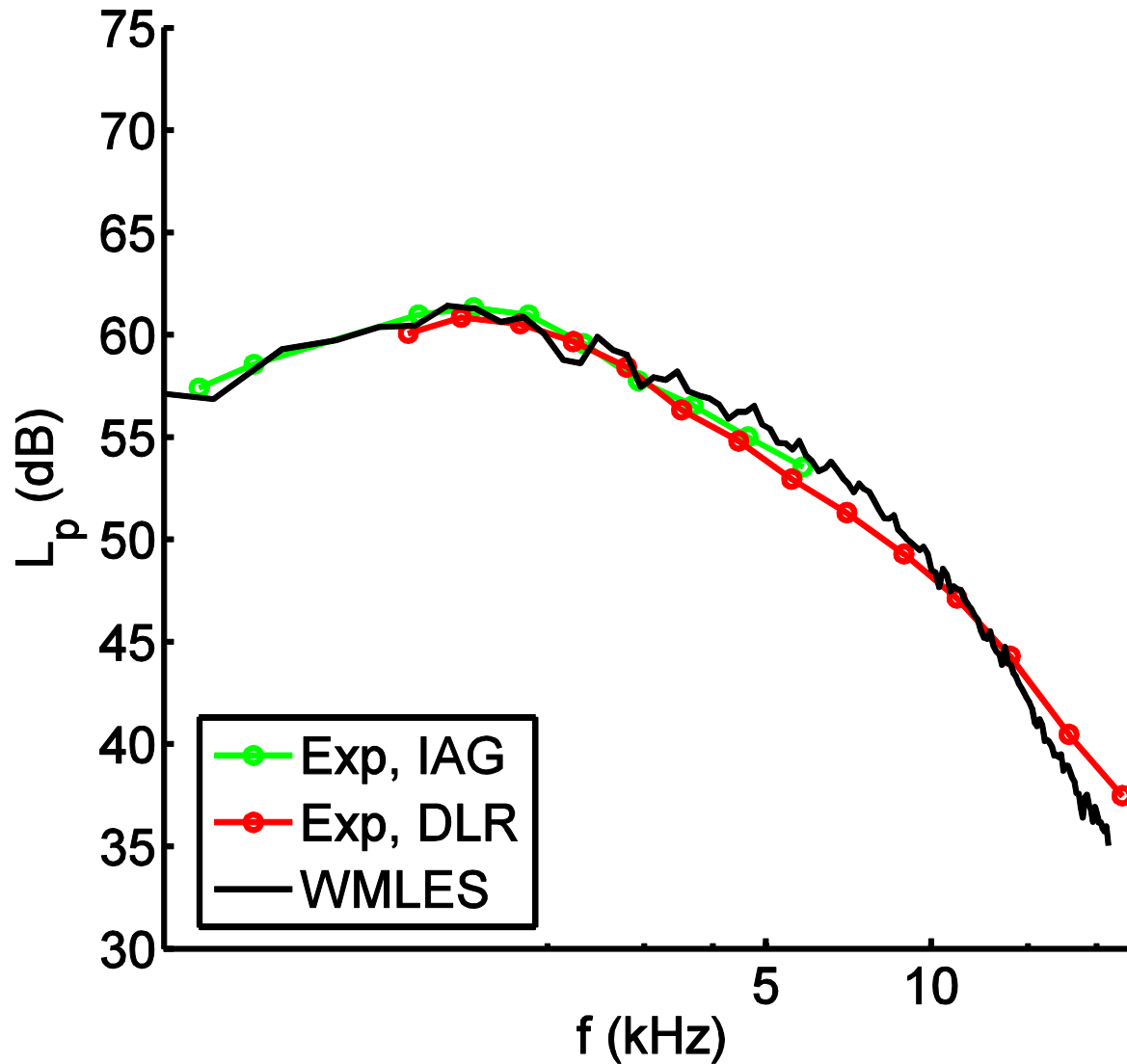
Trailing edge noise predictions at full-scale Reynolds number: The BANC workshop

Configuration	Airfoil	AoA	Reynolds Number	Mach Number	Transition location
BANC 1	NACA0012	0°	1.50M	0.1664	0.065c
BANC 2	NACA0012	4°	1.50M	0.1641	0.065c
BANC 3	NACA0012	6°	1.50M	0.1597	0.060c/0.070c (SS/PS)
BANC 4	NACA0012	0°	1.00M	0.1118	0.065c
BANC 5	DU96	4°	1.13M	0.1730	0.12c/0.15c (SS/PS)

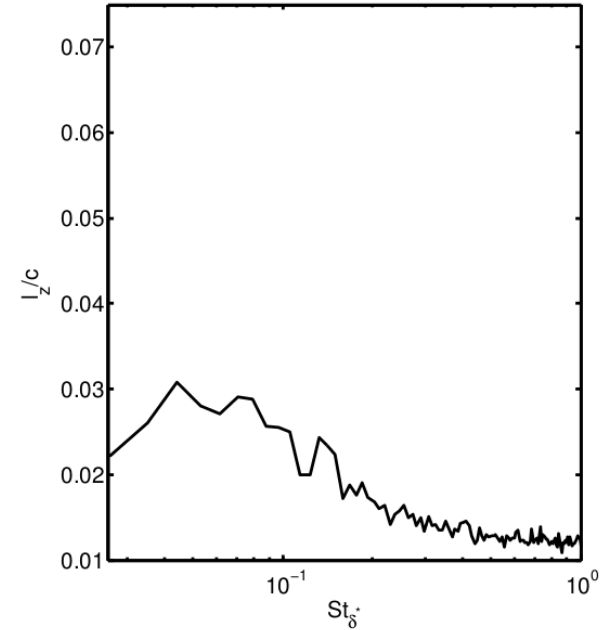
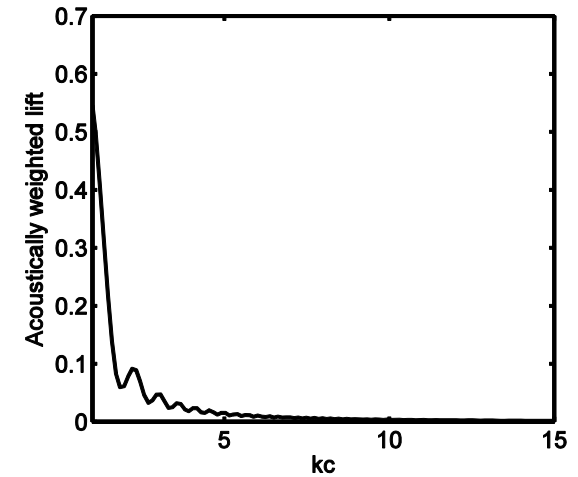
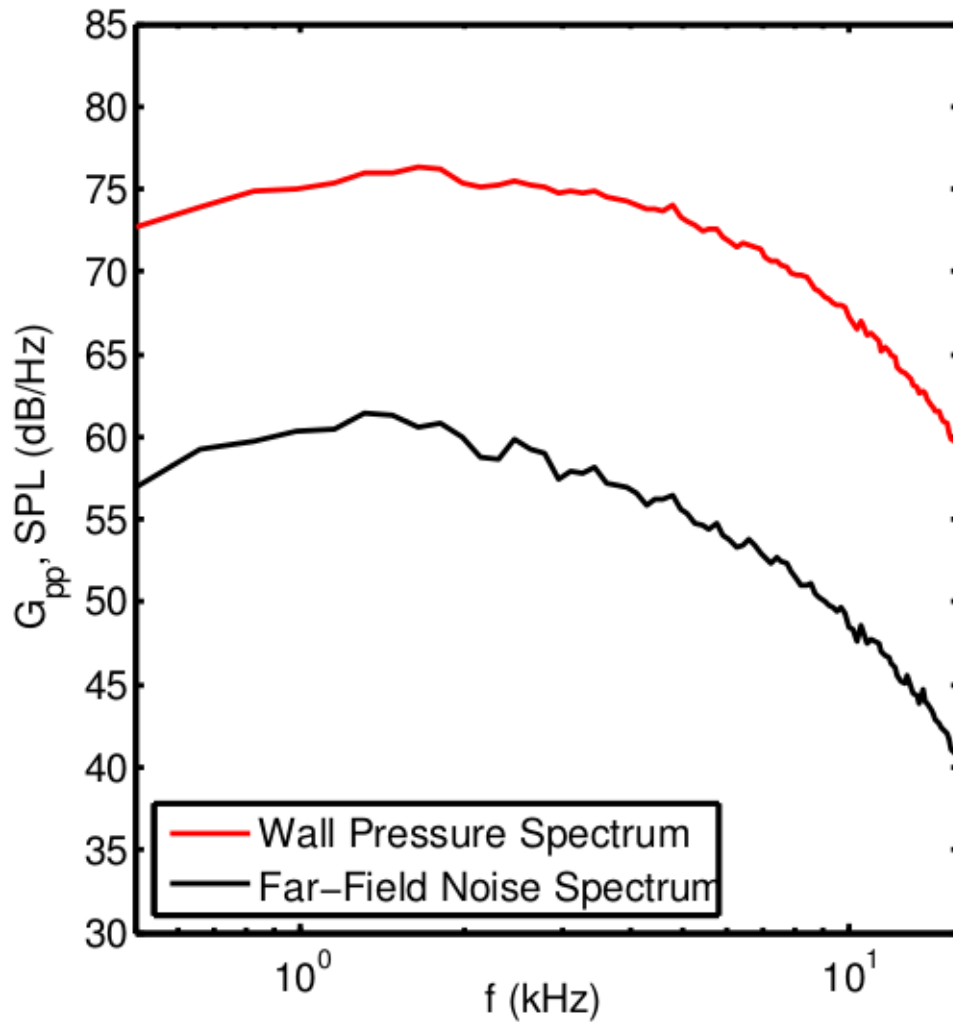
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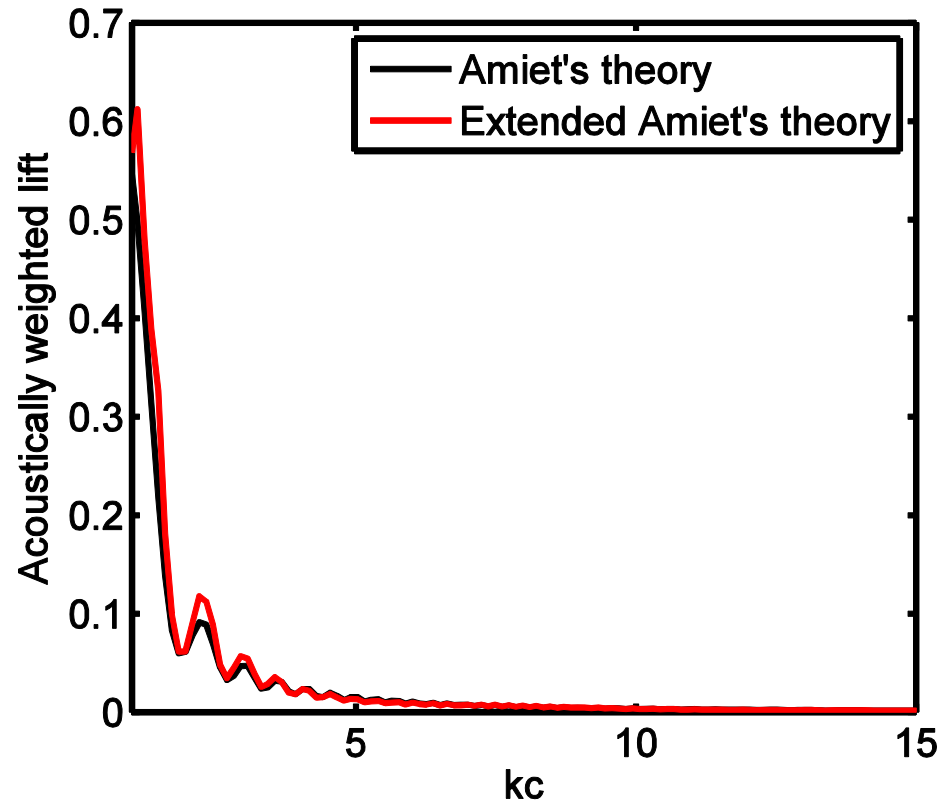
BANC 1 - NACA 0012, $Re = 1.5M$, $M = 0.1664$, $AoA = 0^\circ$



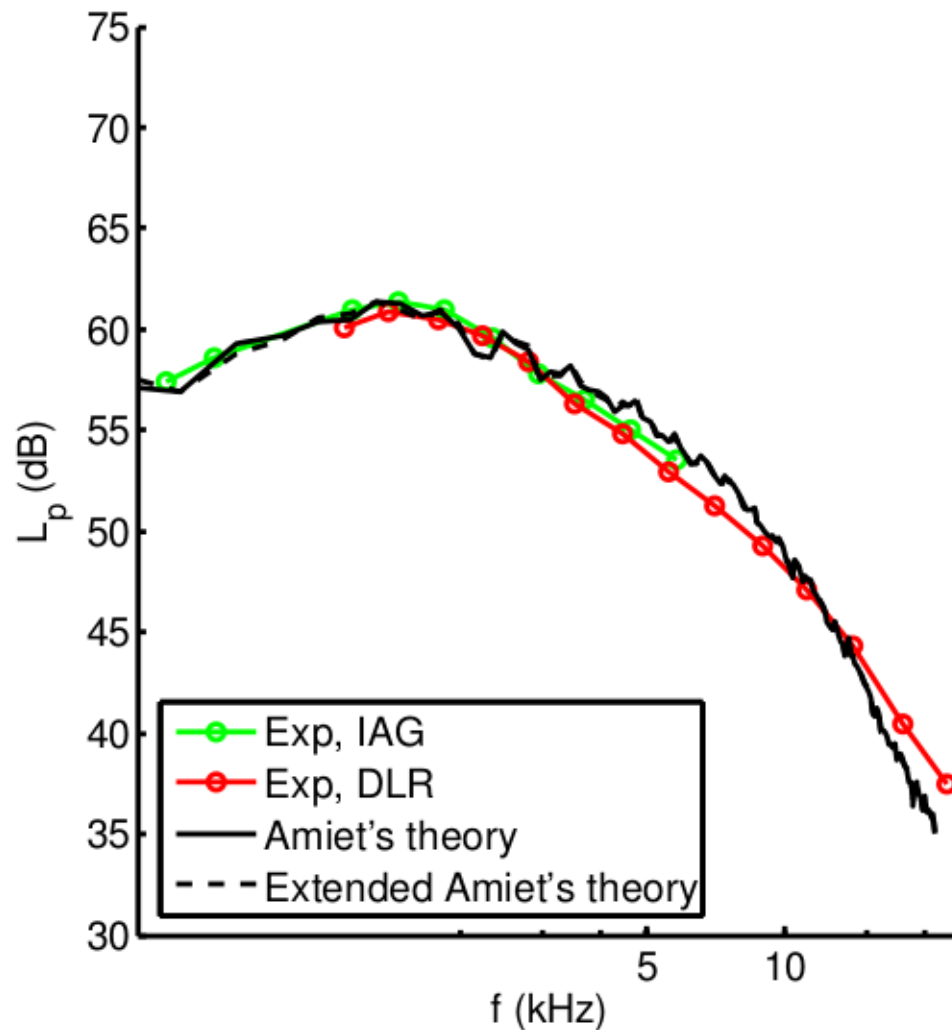
Interpreting the far-field noise spectrum



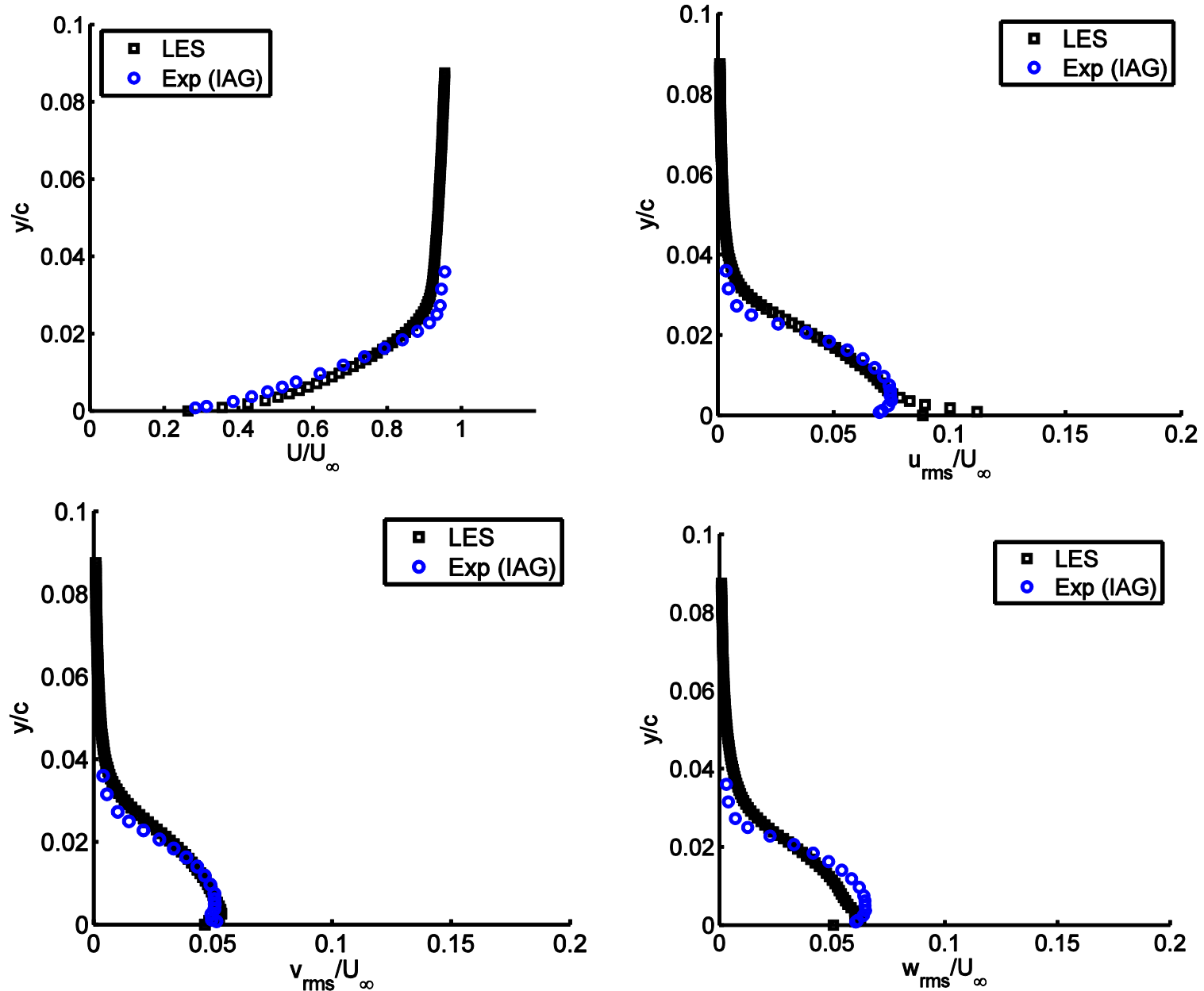
Is leading edge back-scattering important?



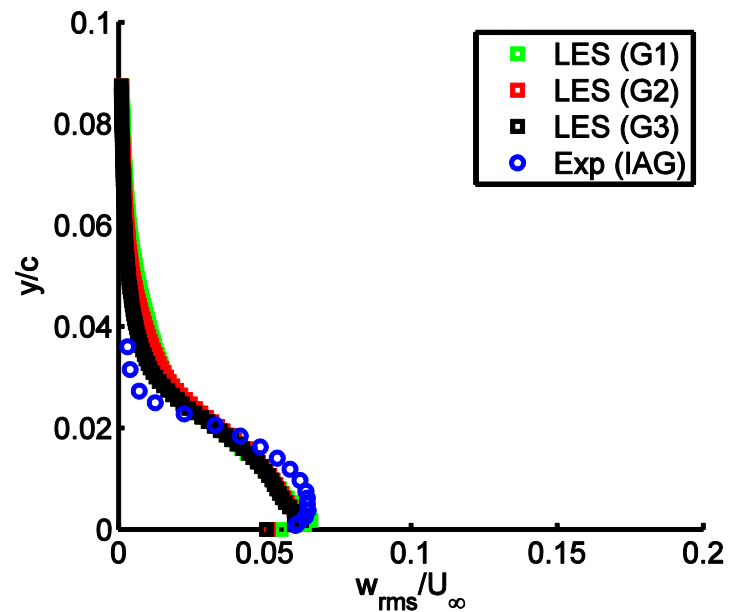
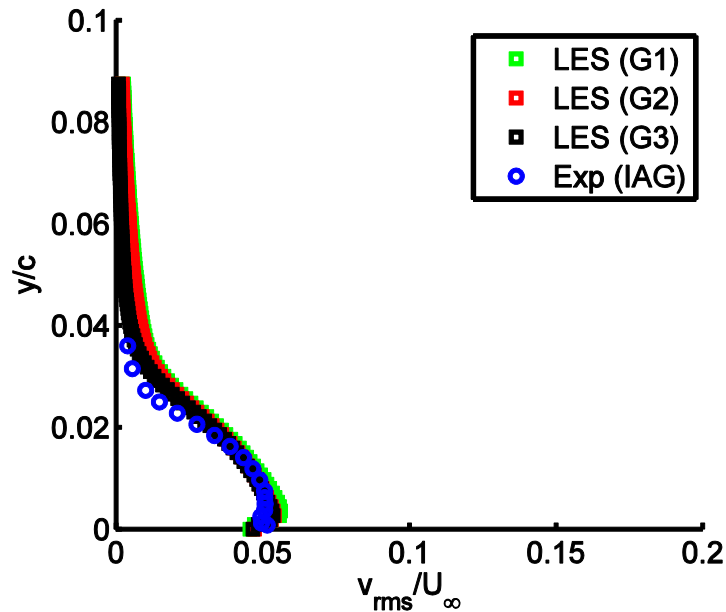
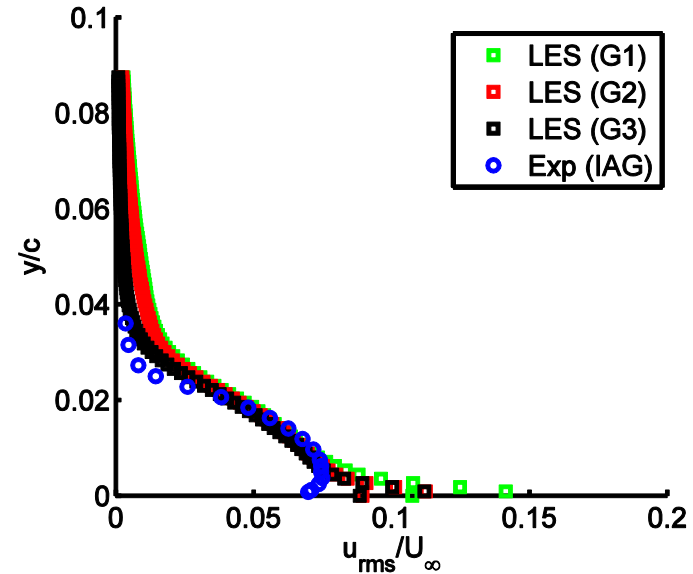
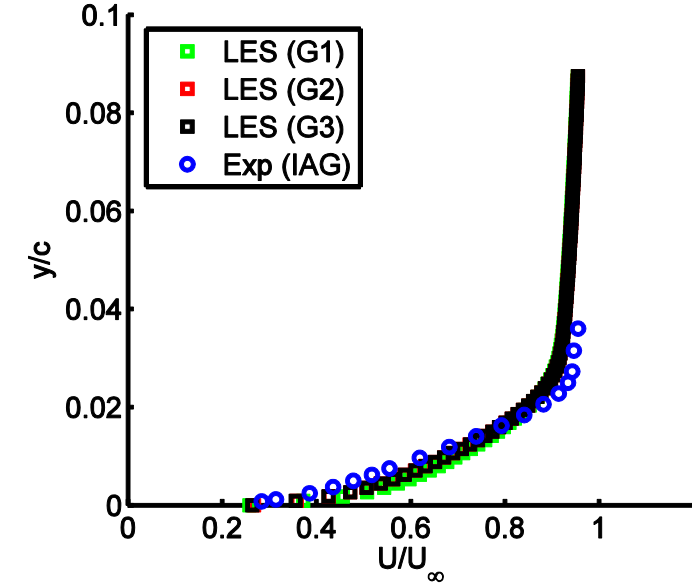
Is leading edge back-scattering important?



Comparison of near wake flow-field to measurements



Sensitivity to grid resolution



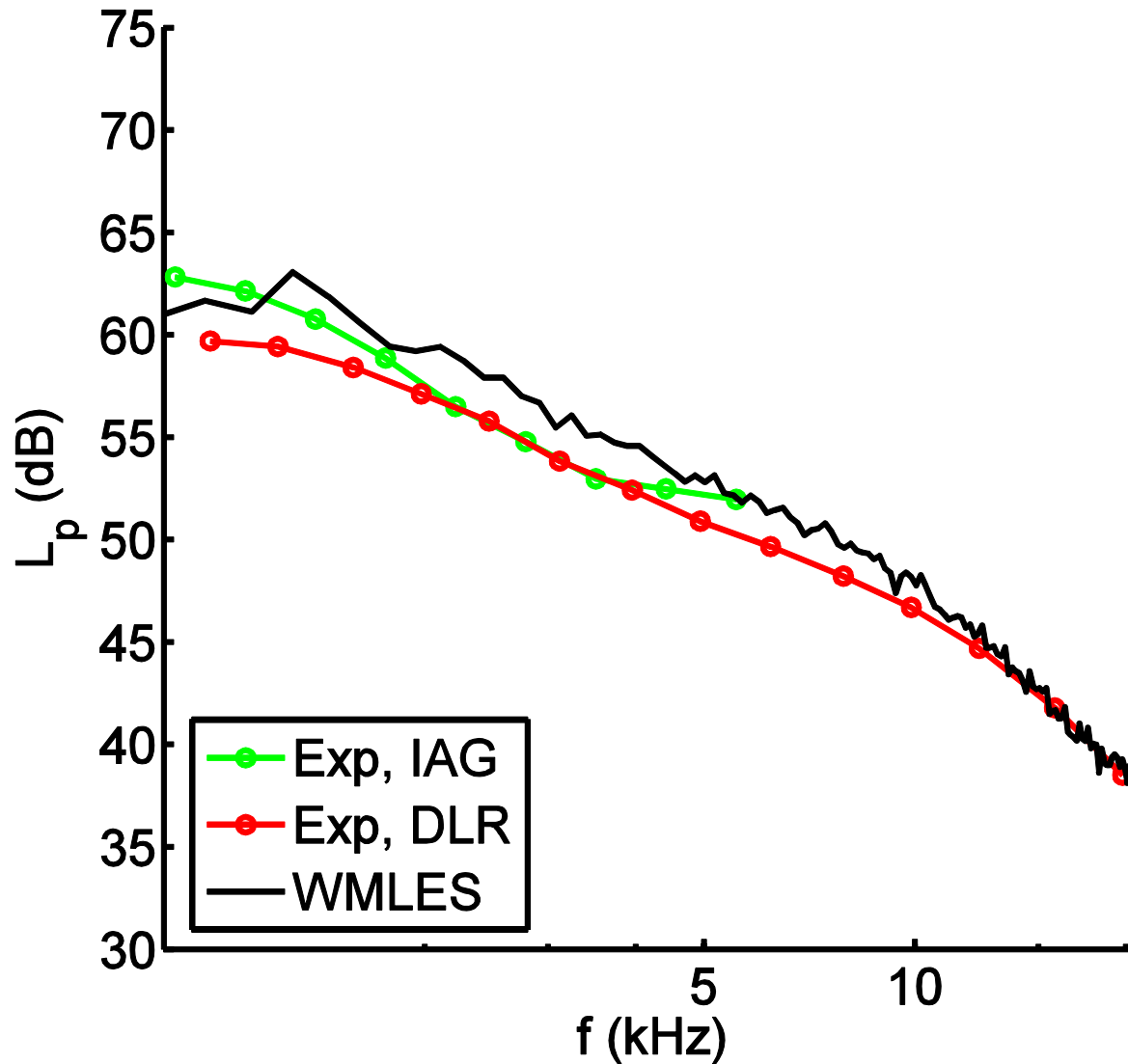
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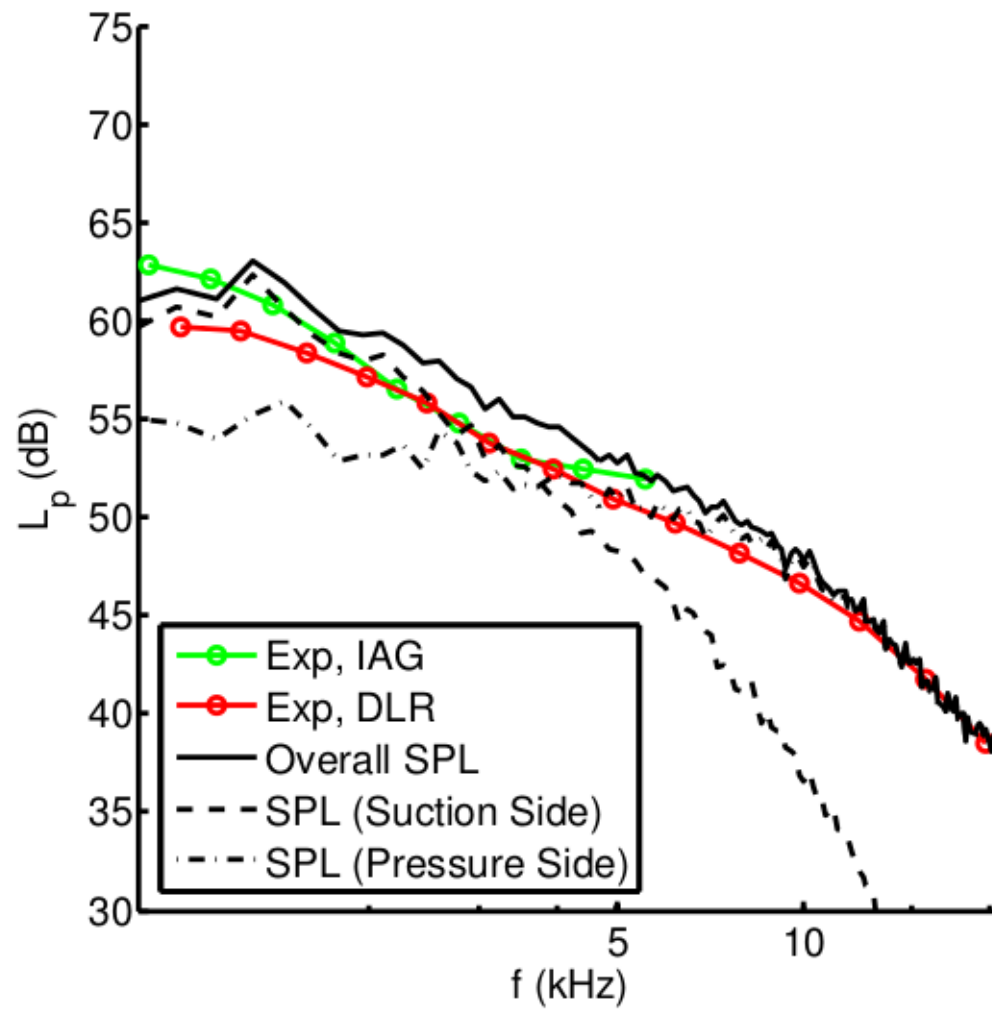
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BANC 3 - NACA 0012, $Re = 1.5M$, $M = 0.1597$, $AoA = 6^\circ$



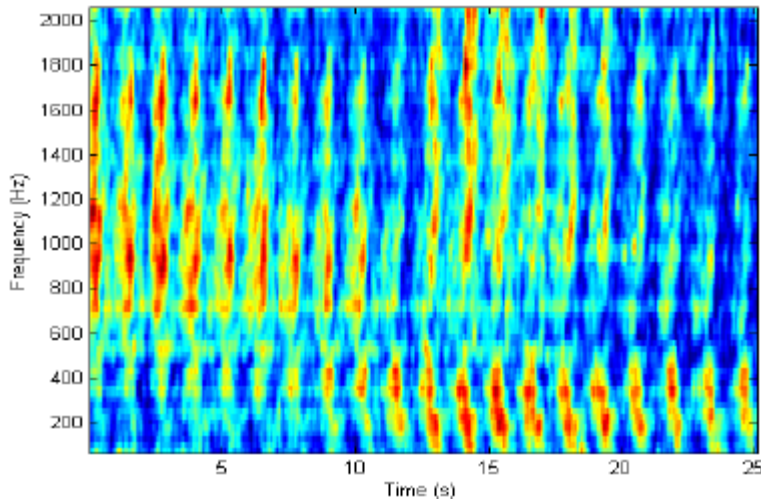
The effect of loading



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- Why Wall Modeled LES (WMLES)?
- WMLES Methodology
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- WMLES of trailing edge noise at high Re
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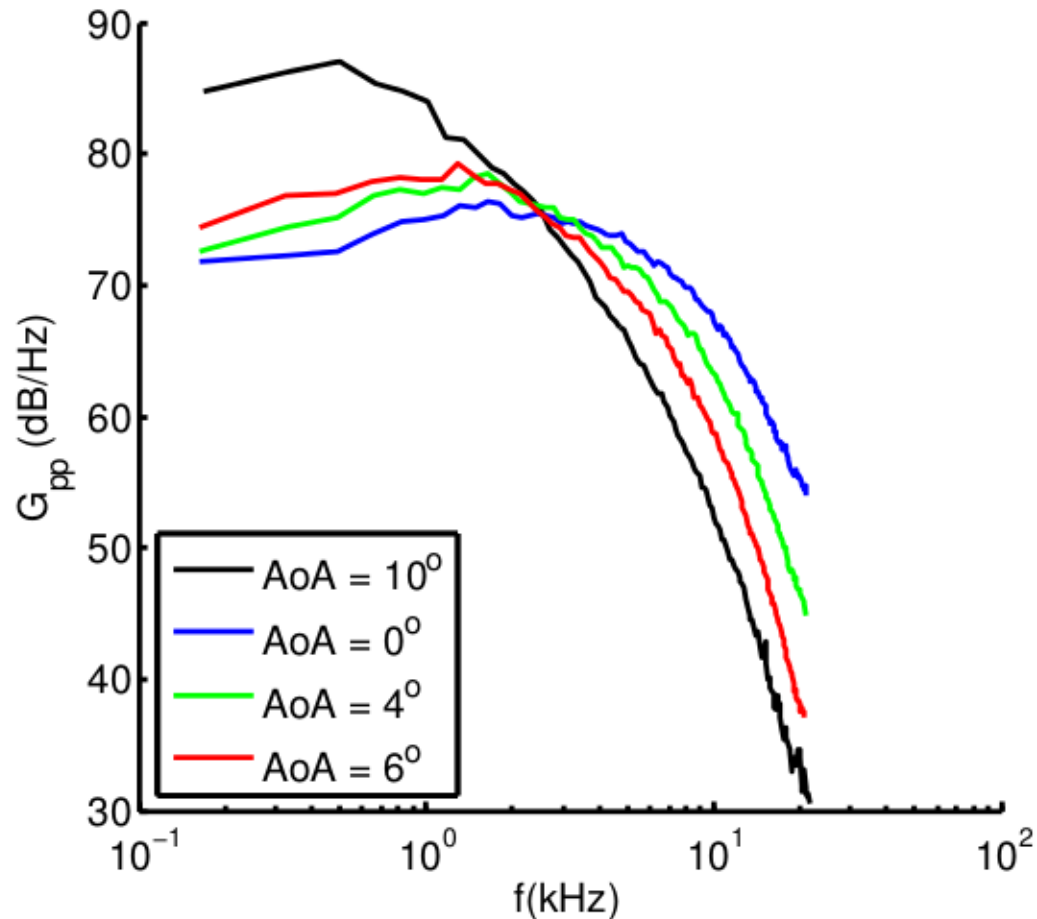
Motivation: *Other* Amplitude modulation (OAM) of wind turbine noise



Spectrogram of wind turbine noise shows intense, intermittent, *thumping* noise believed to be caused by dynamic stall of wind turbine blades.

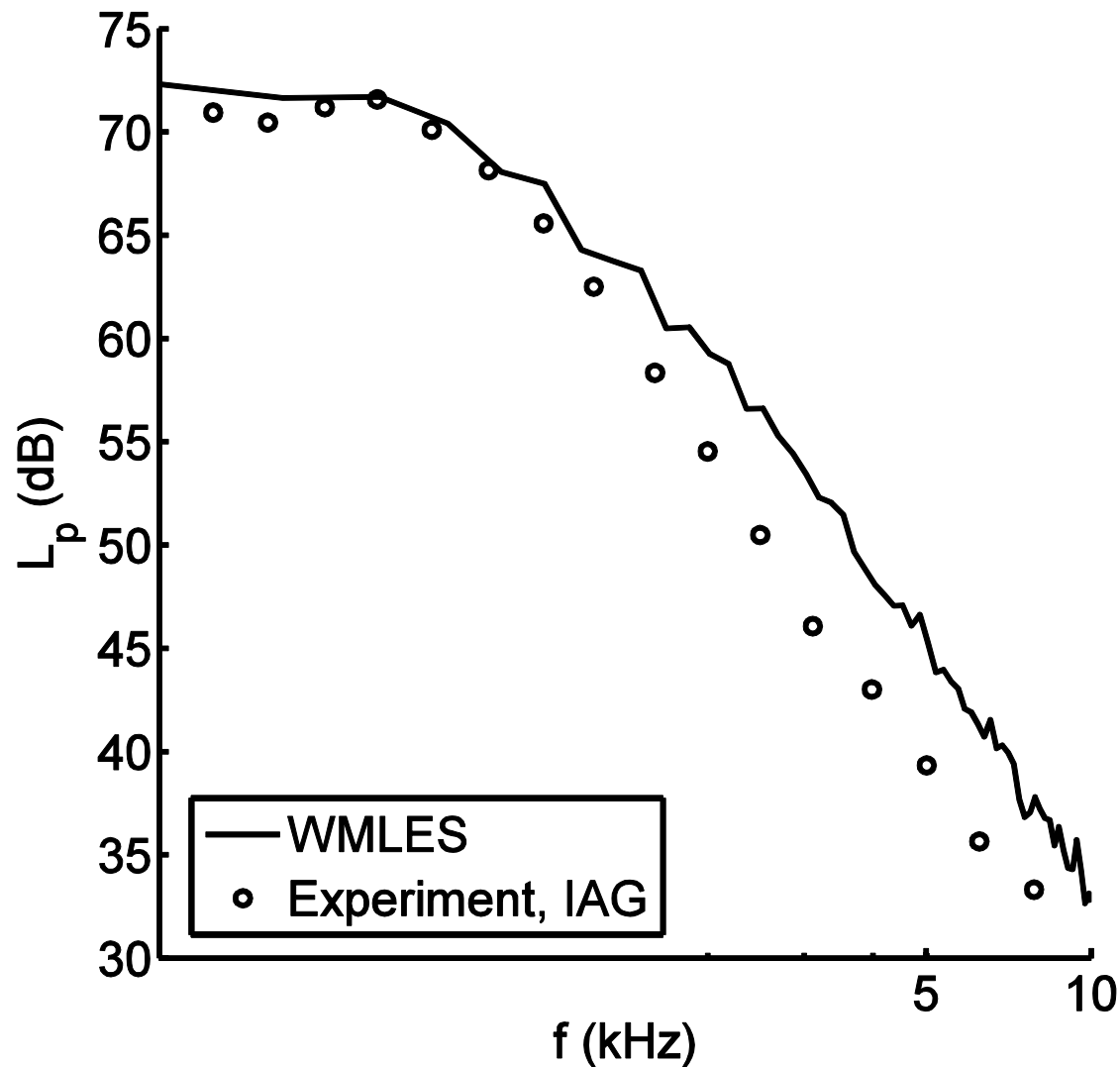
- High levels of amplitude modulation (AM) at large distances *downwind* or *upwind*
- Level and *character* of AM altered
- Increase in low-frequency content
- Enhanced modulation depth
- *Transient*, *dynamic* stall believed to be responsible
- Stall noise prediction – a pacing item (Laratro *et al.*, 2014)

What happens to fluctuating wall pressure at higher AoA?



Noise generated by an airfoil in *near* stall configuration

- NACA 0012, $Re = 1.5M$, $M = 0.16$, $AoA = 10^\circ$



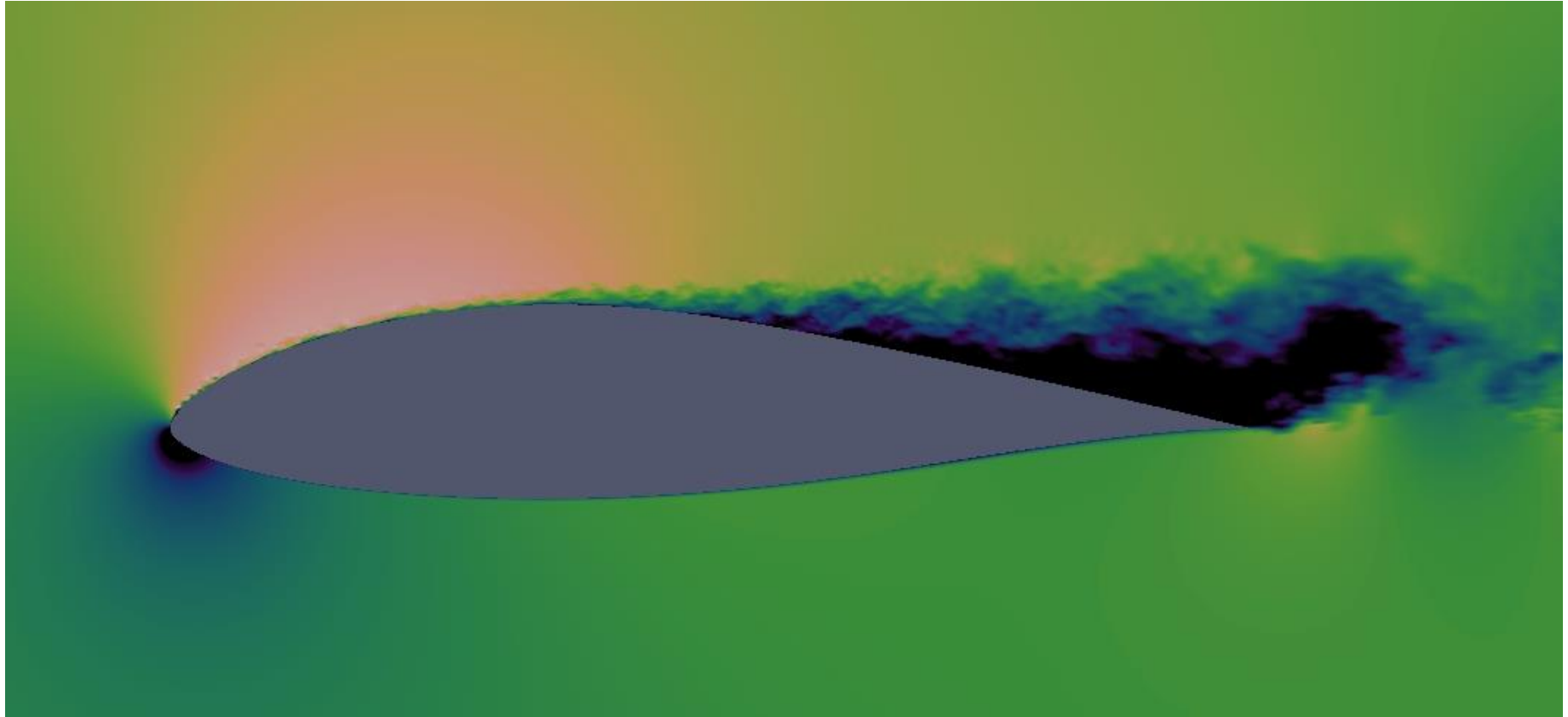
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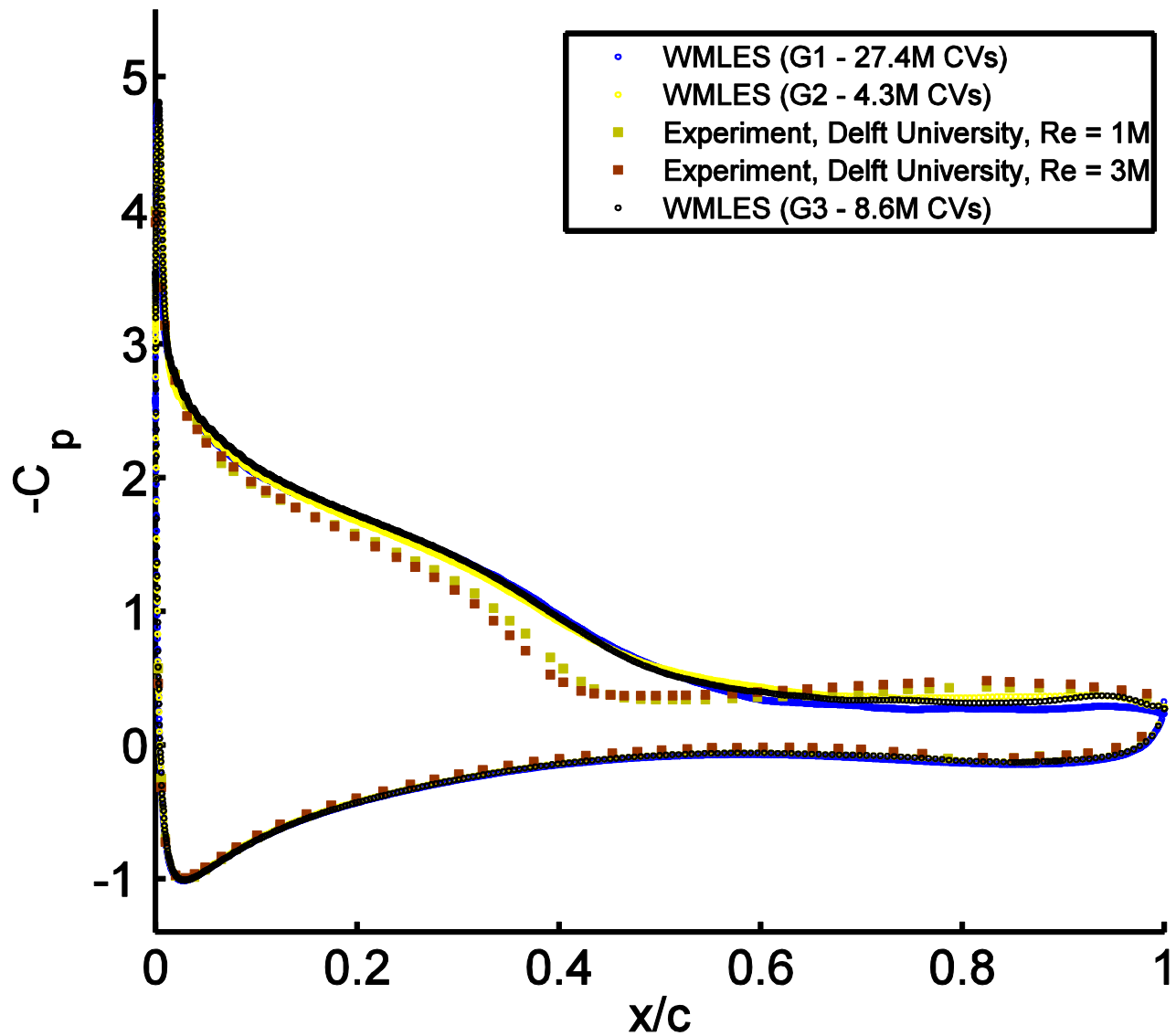
WMLES of turbulent flow past a DU96 airfoil in stall

- Configuration – DU96-W-180 airfoil at an angle of attack of 13.2 degrees, chord based Reynolds number of 1.5M
- Comparisons made with experiments from Delft University (Courtesy: Dr. N. Timmer)

Flow Visualization: Contours of streamwise velocity (Negative values intentionally saturated to visualize reverse flow regions better)



Comparison with Experiments

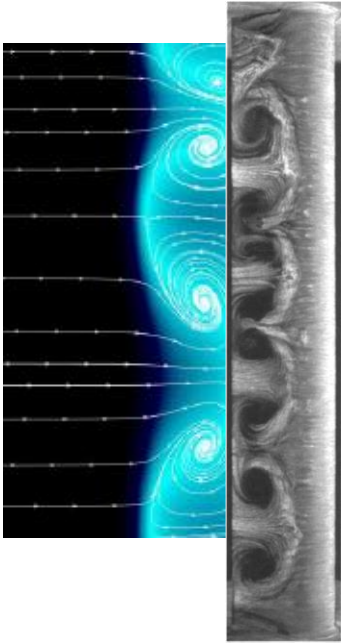


Motivation for large span calculation

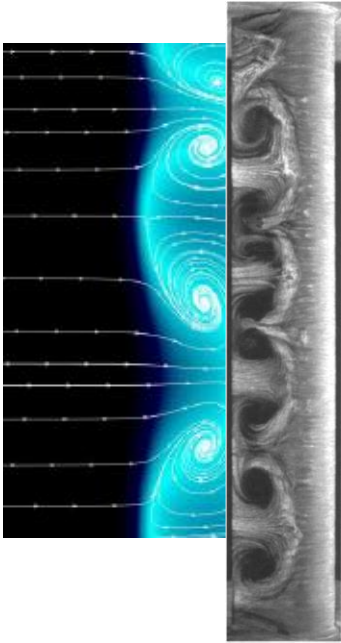
Dataset	Lift Coefficient
WMLES	1.22+/-0.01*
Delft (Re = 1M, AoA = 13.625)	1.109
Delft (Re = 2M, AoA = 13.13)	1.12
Delft (Re = 3M, AoA = 13.62)	1.105
RANS (Re = 1.5M, AoA = 13.2)	1.3915

- **WMLES over-predicts lift by 10%**
- RANS over-predicts lift by 25%

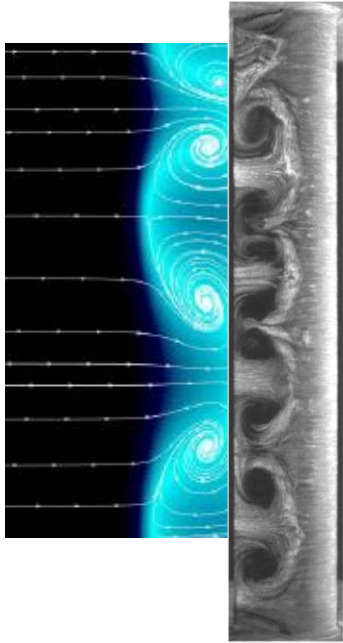
*From calculations done on three different grids



- Are large-scale 3D flow instabilities important?
- Are large-span calculations *without* end-wall effects useful?

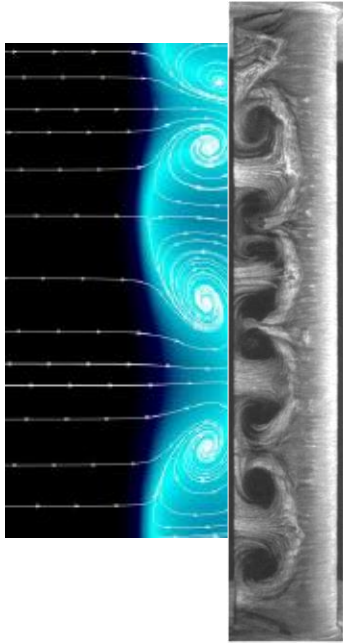


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- Yes – Stall cells affected by end-walls, but *not* caused by it (cf. Spalart (2014))



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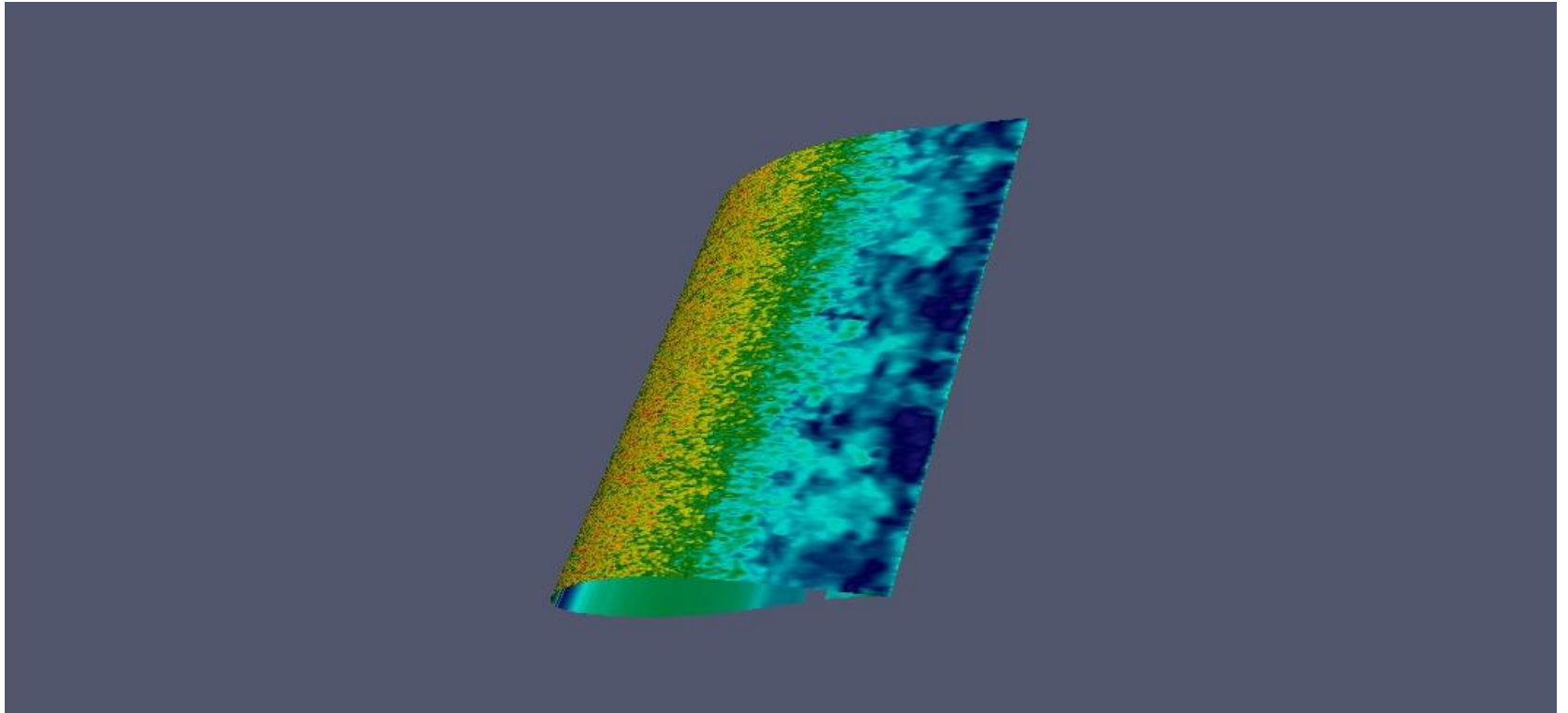
Grid	Domain size	Grid points
G1	20Cx20Cx0.12C	~27.4M
G2	20Cx20Cx0.12C	~4.3M
G3	20Cx20Cx0.12C	~8.6M
G4	20Cx20Cx1.2C	~40.5M



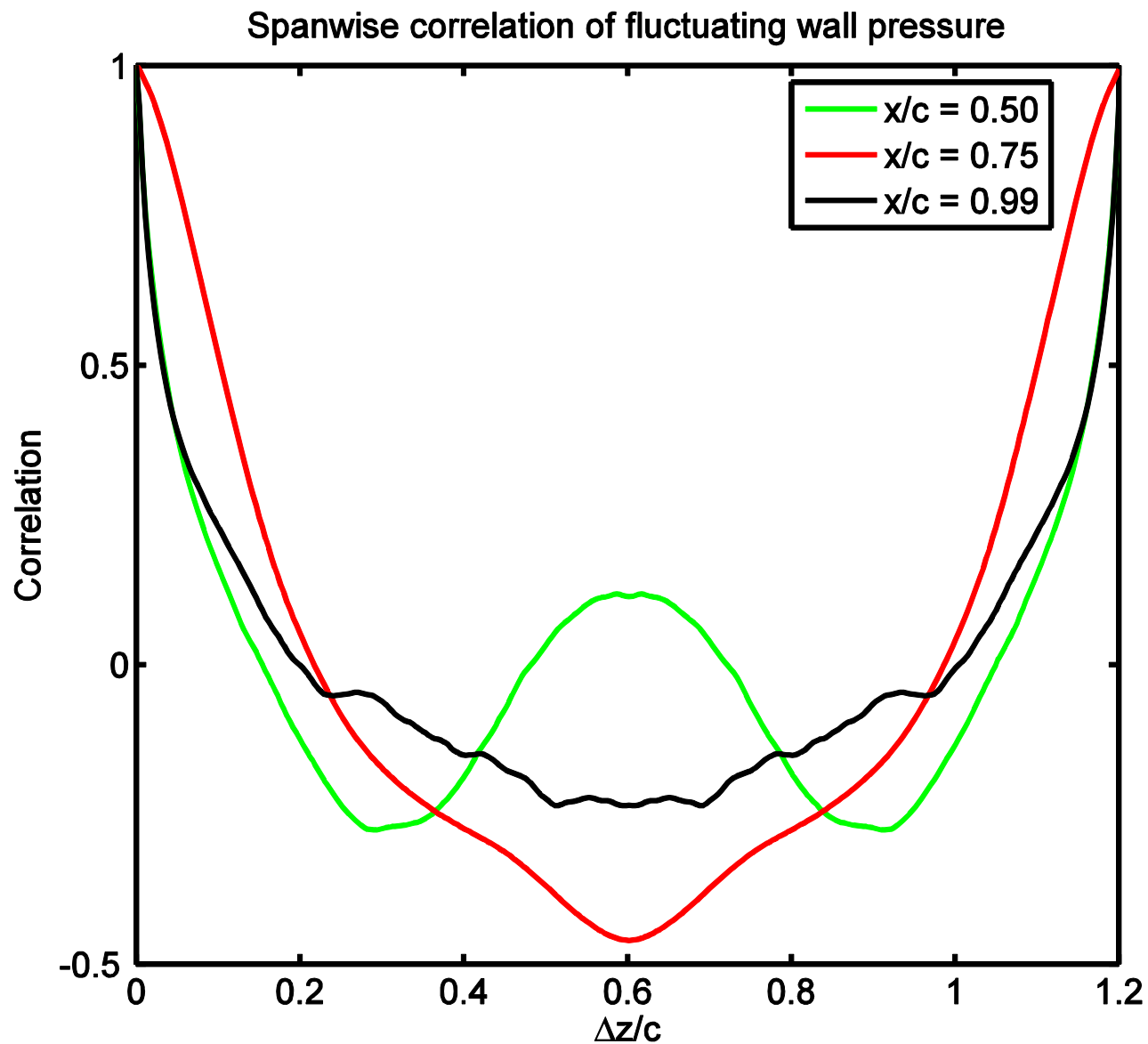
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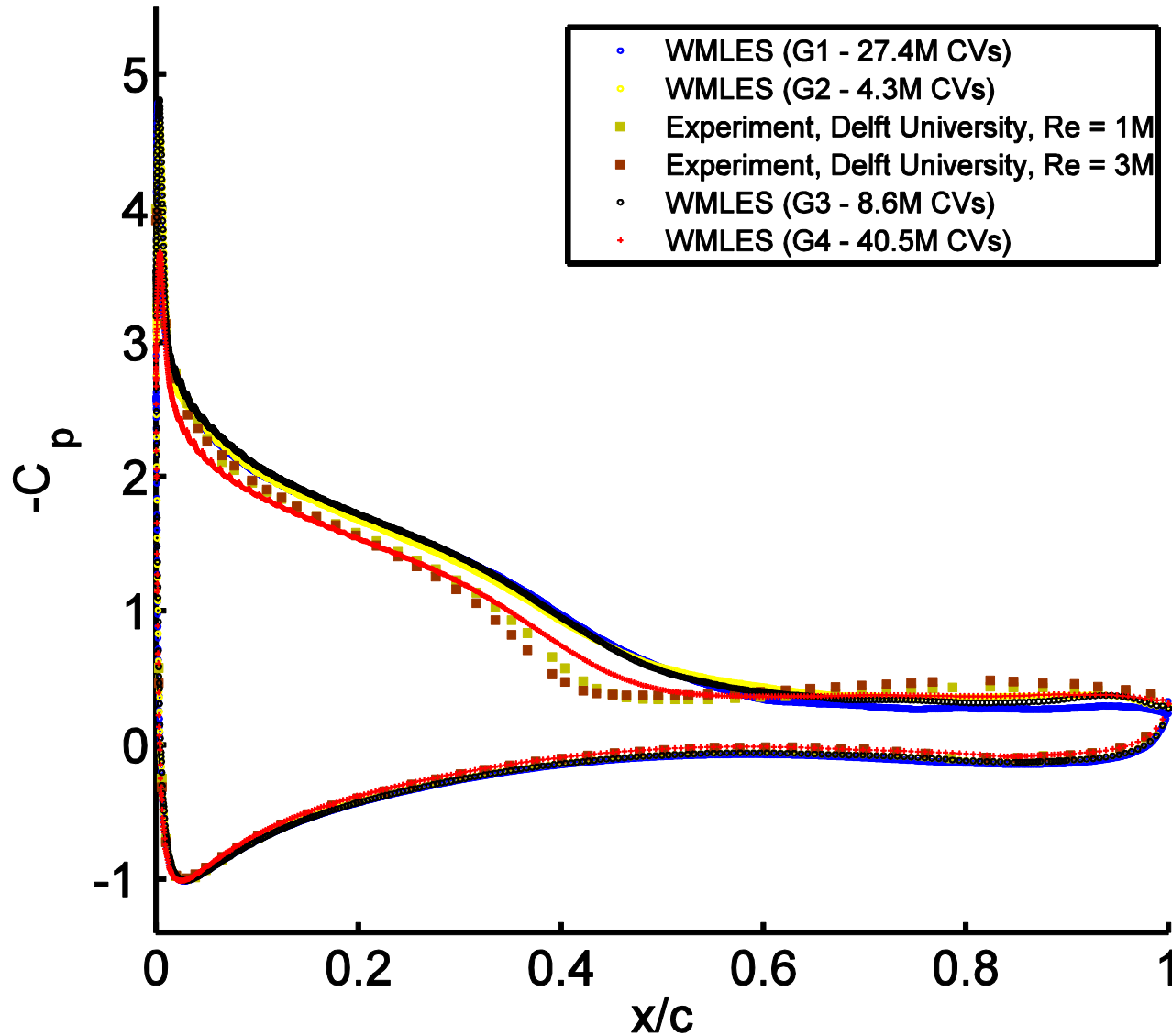
Stall Cells



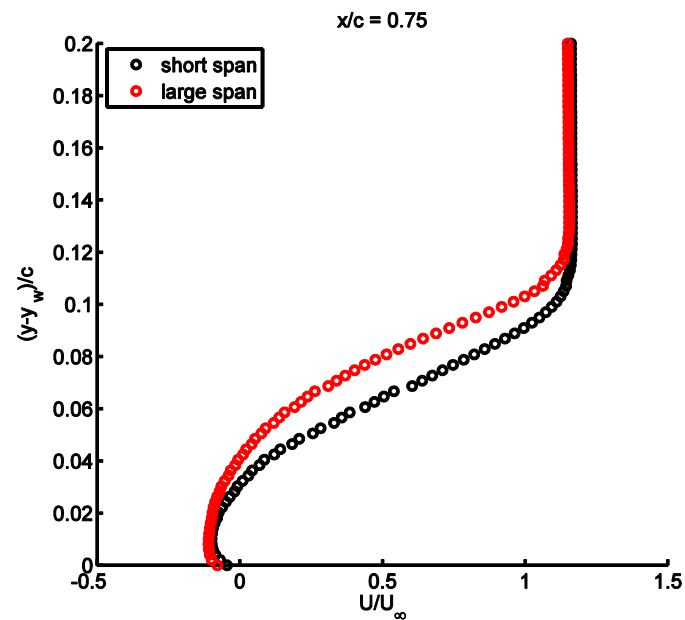
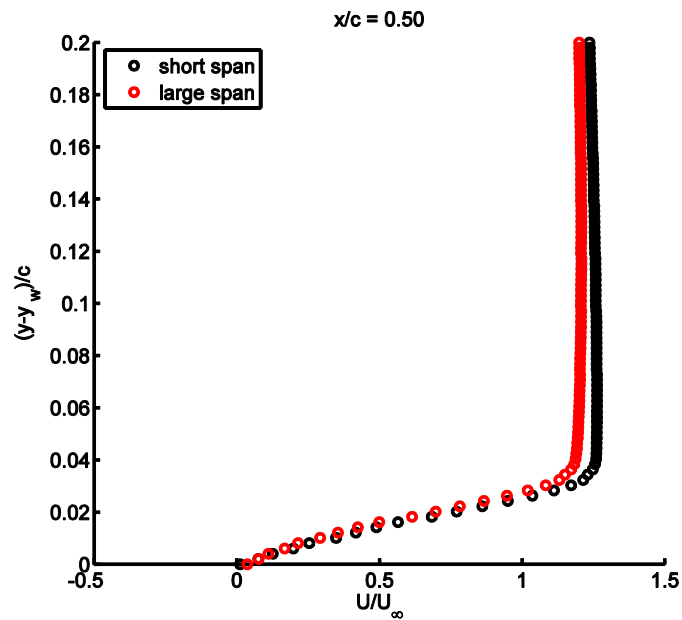
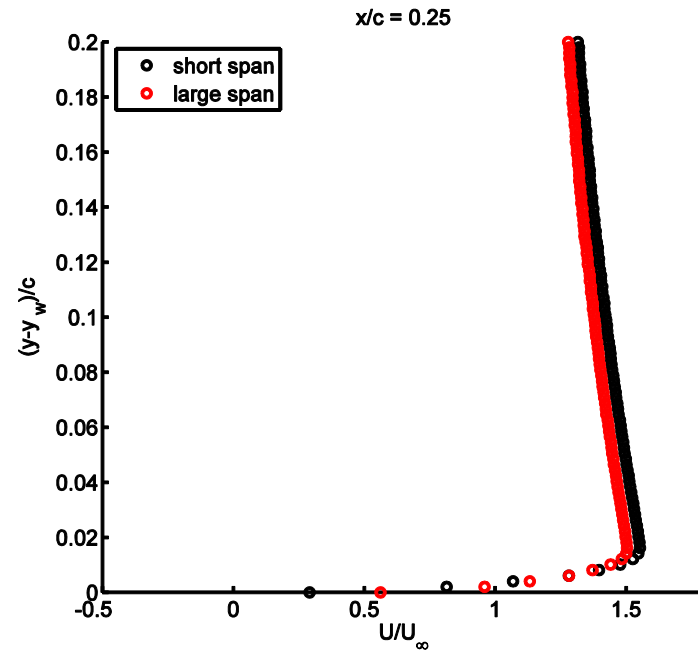
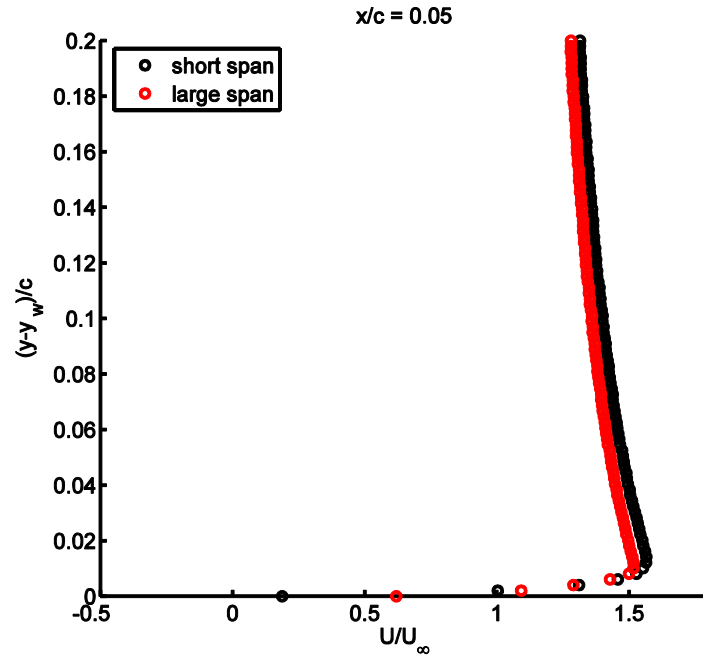
Large-scale 3D flow instability



Comparison with Experiments



Boundary layer profiles on suction side



Comparison of C_L predictions

Dataset	Lift Coefficient
WMLES (short-span)	1.22+/-0.01*
WMLES (large-span)	1.0754
Delft (Re = 1M, AoA = 13.625)	1.109
Delft (Re = 2M, AoA = 13.13)	1.12
Delft (Re = 3M, AoA = 13.62)	1.105
RANS (Re = 1.5M, AoA = 13.2)	1.3915

- **WMLES (large-span) prediction within 3% of measurements**

*From calculations done on three different grids

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Conclusions

- *First* successful prediction of trailing edge noise from first principles at *full scale* Reynolds numbers
- Successful prediction of noise generated by an airfoil in the near stall regime
- Aerodynamic stall of a wind turbine airfoil at full-scale Reynolds numbers using WMLES – Novel large span calculation shows evidence for *stall cells*

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Acknowledgements



GE Global Research



ASCR Leadership
Computing Challenge

Flow Simulation

- Node-based finite volume scheme
- Implicit time advancement
- Second-order accurate in space and time
- Minimally dissipative – relies on discrete kinetic energy conservation for numerical stability
- Low-Mach, *weakly compressible* formulation
- High-frequency acoustic waves filtered out, low frequency acoustic waves retained
- Vreman model for subgrid scales of turbulence
- BCs – stress BC from wall model on the airfoil surface, Sponge BC at far-field boundaries to minimize spurious reflections
- Steady suction/blowing to force transition to turbulence

Far-field noise prediction

- Ffowcs Williams Hawkings Equation
- Amiet's theory, Extended Amiet's theory with leading edge back-scattering corrections from Roger and Moreau
- Chase-Chandiramani-Howe diffraction theory
- Finite-chord and finite-thickness effects investigated

WMLES of turbulent channel flow, $Re_\tau \sim 590$, DNS $\sim 25M$ points, WMLES $\sim 1M$ points

